CAMP Working Paper Series No 8/2022

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December 29, 2022

Abstract

For western economies a long-forgotten phenomenon is on the horizon: rising inflation rates. We propose a novel approach christened D^2ML to identify drivers of national inflation. D^2ML combines machine learning for model selection with time dependent data and graphical models to estimate the inverse of the covariance matrix, which is then used to identify dominant drivers. Using a dataset of 33 countries, we find that the US inflation rate and oil prices are dominant drivers of national inflation rates. For a more general framework, we carry out Monte Carlo simulations to show that our estimator correctly identifies dominant drivers.

JEL Codes: E31, C22, C23, C55.

Keywords: Inflation; Time Series; Machine Learning; LASSO; High dimensional data; Dominant Units;

1 Introduction

The late 1990s marked the start of a period with low inflation rates across the world (Rogoff, 2003) with the exception of the years around the Great Financial crisis. The emergence of the COVID19 pandemic and related supply chain issues brought inflation back to the headlines. The Russian invasion of Ukraine

^{*}We are grateful for many comments from participants of the 19th International Workshop on Spatial Econometrics and Statistics, 27th International Conference on Computing in Economics and Finance, 2022 Panel Data Conference, seminar participants from Lund University and BI Norwegian Business School. We also appreciate helpful comments from Yigit Aydede, Vasilis Sarafids. This paper is part of the research activities at the Centre for Applied Macroeconomics and Commodity Prices (CAMP) at the BI Norwegian Business School. The Authors acknowledge financial support from Italian Ministry MIUR under the PRIN project Hi-Di NET - Econometric Analysis of High Dimensional Models with Network Structures in Macroeconomics and Finance (grant 2017TA7TYC).

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and the resulting increases in energy prices further fuelled inflation, especially in western countries. While it is well understood that national inflation is driven by national factors (Auer et al., 2019), the effects of spillovers across countries are less researched. Auer et al. (2019) find that international input linkages synchronize inflation rates between countries. Bataa et al. (2013) present evidence that the Euro Area leads inflation in North America and that inflation rates are more synchronized since the 1980s. The effect of global factors or common factors on national inflation is well understood. Ciccarelli and Mojon (2010) establish that 2/3 of national inflation is due to global inflation. However global inflation is not a stand in for common shocks such as changes in commodity prices and they find that no country is leading global inflation.

To fill this gap in the literature, we use a novel approach to identify dominant drivers influencing national inflation using the GVAR database (Mehdi Raissi and Mohaddes, 2020). Drivers can be other countries' inflation rate or macroeconomic variables of the same or other countries. We find that the inflation rates in the United States and oil prices changes have a dominant effect on national inflation rates in a set of 33 countries. Our results are robust to different estimation methods and specifications. An advantage of our approach is that it allows to identify dominant drivers even if the number of variables is larger than the number of observations over time. Inflation can be influenced by foreign inflation and domestic and foreign factors, such as asset prices or interest rates. Thus the number of potential variables can be larger than the number of observations over time when estimating a specific national inflation series.

Our approach relies on the inverse of the covariance matrix of the data and consists of two steps. The first step is based on Meinshausen and Bühlmann (2006) and Sulaimanov and Koeppl (2016) and uses a graphical model to estimate the inverse of the covariance matrix, the precision or concentration matrix. In a graphical model nodes (variables) are connected by edges (connections). No connection between two nodes translates to a zero element in the concentration matrix and indicates independence between the variables. A non-zero in the concentration matrix implies dependence or a common edge between two nodes in the graphical model. Hence estimating the linkages between units using a graphical model is informative about the structure or sparseness of the concentration matrix. The entries of the concentration matrix can be represented by partial correlations and are therefore related to estimated regression coefficients (Sulaimanov and Koeppl, 2016). Meinshausen and Bühlmann (2006) and Sulaimanov and Koeppl (2016) propose to use the least absolute shrinkage and selection operator (LASSO) estimator to estimate the graphical model and then use post LASSO OLS to estimate the elements of the concentration matrix. We extend the approach by Meinshausen and Bühlmann (2006) and Sulaimanov and Koeppl (2016) to time dependent data by combining it with either the rigorous LASSO (Bickel et al., 2009; Belloni et al., 2016; Chernozhukov et al.,

¹Dominant drivers are often labelled as dominant series or units. Brownlees and Mesters (2021) call them *granular series* and Kapetanios et al. (2021) call them *units with pervasive effects*. Throughout the paper we will refer to them as *dominant drivers*.

2019; Ahrens, Aitken, Ditzen, Ersoy, Kohns and Schaffer, 2020) or the adaptive LASSO estimator (Zou, 2006; Medeiros and Mendes, 2016). The advantage is of LASSO is its applicability to data where the time dimension is smaller than the number of series or units.

The second step is the selection of the dominant drivers. We use the procedure in Brownlees and Mesters (2021), henceforth BM, to select the dominant drivers from the estimated concentration matrix. In the BM procedure, the column norms of the concentration matrix are ordered by their size and the dominant drivers identified using a criterion similar to the eigenvalue ratio criterion in Ahn and Horenstein (2013). We propose to use the heteroskedastic and autocorrelation robust rigorous LASSO and the adaptive LASSO to estimate the graphical model. Based on the linkages, post-LASSO OLS estimates the entries of the concentration matrix. Monte Carlo simulation results show that our proposed extension correctly identifies the dominant drivers. Since our approach relies on machine learning methods to identify the dominant drivers, we call it *Dominant Drivers by Machine Learning*, D^2ML .

The contributions of D^2ML are threefold: First, it can be applied to data which has more variables than observations, a disadvantage of the method by Brownlees and Mesters (2021). Secondly it is computationally more simple than the method in Kapetanios et al. (2021) and requires less assumptions. Finally, it can be applied to various types of data as shown in our Monte Carlo Simulations.

Dominant drivers have a strong influence on other units or series and their identification received growing attention in recent years. In an infinite VAR Chudik and Pesaran (2013) suggest to model the dominant driver as a common factor. Kapetanios et al. (2021) propose a sequential multiple testing approach to identify drivers with pervasive effects in a large panel model. The underlying idea is to identify the drivers using their error variance, on which the multiple testing approach (Bailey et al., 2020) is applied to. Parker and Sul (2016) identify dominant drivers by analysing the residual variances of regressions of principal components on the time series and other principal components. Pesaran and Yang (2020) identify dominant drivers in production networks using a criterion similar to the exponent of cross-section dependence. Brownlees and Mesters (2021) define a dominant driver by the means of the column norms of the inverse of the covariance matrix and a selection criteria. Their criteria requires to invert the covariance matrix and is therefore only applicable to datasets with N < T.

Our work extends the literature on inflation and on the identification of dominant drivers. The results from the empirical application show that the inflation in the US and oil prices act as a dominating series. We do not find evidence that real GDP, equity prices, exchange rates and interest rates have a dominating effect on national inflation.

The remaining part of this paper is structured as follows: the next section describes the theoretical background, followed by a discussion our D^2ML . We provide evidence for our approach using Monte Carlo Simulations and discuss our findings of US and oil prices dominating national inflation rates.

The notation throughout this paper is as follows: matrices are in capital and

bold, such as \boldsymbol{X} , vectors are in lower-case letters and bold, \boldsymbol{x} and scalars are lower-case x. Time indices are denoted by t=,1...,T, unit indices by i=1,...,N and the number of variables are defined as k=1,...,K. $||\boldsymbol{X}_i||$ refers to the i-th column norm of matrix \boldsymbol{X} .

2 The D^2ML approach

This section defines the *Dominant Drivers by Machine Learning* (D^2ML) two step approach to identify dominant drivers in large panel models. In the first step we identify the links between the units and in the second step we select the dominant drivers.

In the first step, called the *network selection step*, henceforth NSS, we recover the network structure using a graphical model and then estimate the concentration matrix. A graphical model links the estimation of a network in the form of nodes connected by edges and the structure of the concentration matrix, for a summary see Meinshausen and Bühlmann (2006); Sulaimanov and Koeppl (2016); Friedman et al. (2008). The link between the graphical model and the inverse of the covariance matrix is that if two series are independent they have a zero partial correlation and are not in the same edge set.

We want to identify the set $\Gamma(N_d)$ of N_d dominant drivers in the $T \times N$ variable X. We define the entries of the dominant drivers as:

$$x_{i,t,d} = u_{i,t}, i \in \Gamma(N_d) (1)$$

and of the non dominant units:

$$x_{i,t,nd} = \sum_{j \in \Gamma(N_d)} \beta_{i,j} x_{j,t} + u_{i,t}, \qquad i \notin \Gamma(N_d)$$
 (2)

where $\beta_{i,j}$ measure how much dominant driver j influences the non-dominant unit i. A unit cannot influence itself, hence $\beta_{i,i} = 0$. $x_{i,t}$ and the iid error component $u_{i,t}$ can be serially correlated but stationary over time and can include common factors. The error component $u_{i,t}$ can also be potentially heteroskedastic. We define the covariance matrix of $\mathbf{X} = (\mathbf{x}_1, ..., \mathbf{x}_N)'$ by $\mathbf{\Sigma}$ and the concentration matrix is $\mathbf{\kappa} = \mathbf{\Sigma}^{-1}$.

Following Meinshausen and Bühlmann (2006) and Sulaimanov and Koeppl (2016) the graphical model is recovered based on the optimisation problem:

$$\hat{\beta}(\lambda)_i = \arg\min_{\beta} \sum_{t=1}^T \left(x_{i,t} - \sum_{j=1, i \neq j}^N x_{j,t} \beta_j \right)^2 + \lambda_i \sum_{j=1}^N \psi_j |\beta_j|$$
 (3)

where $\lambda > 0$ is penalty level (or tuning parameter) and ψ_j is the penalty loading. To estimate Equation (3) and select the penalty level and loading, we

propose two estimator: the rigorous or plug-in LASSO (Bickel et al., 2009; Belloni et al., 2016; Chernozhukov et al., 2019; Ahrens, Aitken, Ditzen, Ersoy, Kohns and Schaffer, 2020) and the adaptive LASSO (Zou, 2006; Medeiros and Mendes, 2016). The rigorous LASSO is a data driven method to select λ . The penalty loading ψ_j is estimated and adjusted to the assumptions of the error variances and can account for clustered error variances (Belloni et al., 2016), heteroskedasticity and autocorrelated errors (Ahrens, Aitken, Ditzen, Ersoy, Kohns and Schaffer, 2020). The adaptive LASSO is a two step method which allows simultaneous estimation and consistent variable selection by weighting the ℓ_1 penalty term, $\sum_{j=1}^{N} \psi_j |\beta_j$. The penalty loading is obtained from an initial regression and the tuning parameter is obtained by cross-validation (CV) or information criteria such as the AIC, BIC, AICC.

Meinshausen and Bühlmann (2006) show that the inverse of the covariance matrix can be estimated for each node or variable individually. This implies that the problem in Equation (3) is repeated for each unit or variable. Depending on the data, the dominant driver can be a specific cross-sectional unit or a variable.

The solution to Equation (3) yields the non-zero elements in each row of the concentration matrix, or in different words it informs which units influence the unit in question, unit i. To construct the concentration matrix, the post-LASSO estimates $\hat{\beta}_{i,j}$ for each cross-section are collected and the $N \times N$ matrix β constructed:

$$\hat{\boldsymbol{\beta}} = \left(\hat{\boldsymbol{\beta}}_1, ..., \hat{\boldsymbol{\beta}}_N\right)' \tag{4}$$

$$\hat{\beta}_{i} = (\hat{\beta}_{i,1}, ..., \hat{\beta}_{i,i-1}, 0, \hat{\beta}_{i,i+1}, ..., \hat{\beta}_{i,N})$$
(5)

Following Sulaimanov and Koeppl (2016) we construct the concentration matrix as:

$$\hat{\kappa} = \hat{\mathbf{D}} \left(\mathbf{I} - \hat{\boldsymbol{\beta}} \right) \tag{6}$$

$$\hat{\mathbf{D}} = diag(\hat{\sigma}_1, ..., \hat{\sigma}_N) \tag{7}$$

where $\hat{\boldsymbol{\beta}}$ is a $N \times N$ matrix of the estimated post-LASSO coefficients from (3) and $\hat{\mathbf{D}}$ is a diagonal matrix with the inverse of the estimated error variances of the i-th regression. The matrix $\hat{\boldsymbol{\beta}}$ will be sparse and the sparseness will carry over to the concentration matrix (Sulaimanov and Koeppl, 2016).

The second step, the *dominant driver selection*, henceforth DDS, is based on Brownlees and Mesters (2021). The authors show that the entries and therefore the column norm of the concentration matrix will be larger for dominant than non-dominant units.²

The problem can be divided into two problems: the estimation of the number of dominant drivers and the identification of which units are dominant drivers.

 $^{^2}$ The same applies to the row norm, for the remainder of this work we will use the column norm.

Brownlees and Mesters (2021) propose to use the eigenvalue ratio criterion from Ahn and Horenstein (2013) to select the number of dominant drivers applied to ordered column norms of the concentration matrix. The number of dominant drivers is defined as:

$$\hat{N}_d = \underset{s=1,\dots,N-1}{\arg\max} ||\hat{\kappa}_{(s)}||/||\hat{\kappa}_{(s+1)}||$$
(8)

where $\hat{\kappa}_{(s)}$ is the s-largest column norm of matrix $\hat{\kappa}$. All units with a larger column norm than column N_d are considered dominant drivers. The number of dominant drivers is a subset of all units and no ratio is assumed.

The NSS step requires the assumptions from Meinshausen and Bühlmann (2006) to ensure oracle properties of the estimator. The oracle properties imply that model selection and estimation of β are unbiased and consistent. The properties are important because otherwise the second step, the DDS, will select falsely non dominant units as dominant drivers. In summary the assumptions for the oracle properties in Meinshausen and Bühlmann (2006) are that the graph is sparse, independence in the error components, correlations are bounded from below and neighbourhood stability. The aim of D^2ML is to identify dominant drivers in high dimensional datasets where the number of cross-sections or variables is larger than the number of time periods. The dominant units are ordered in a block structure as in Brownlees and Mesters (2021), however we explicitly allow for N > T. The column norms of the dominant drivers are larger than a threshold and larger than those of non-dominant units. This is equivalent to a sparse concentration matrix, in which elements of non-dominant units are close to or exactly zero. The graphical model acts a thresholding method to select only the influential connections between units, which then imply a larger column norm in the concentration matrix.³ The second assumption is that the sole source of dependence between units is via the dominant drivers and the residuals are cross-sectionally independent. While this assumption is restrictive, our simulations show that it can be relaxed to a certain degree. The last two assumptions are technical and ensure that the entries of the concentration matrix are not going to infinity and that there are no circle connections between two units via a third one.

There are two notable challenges when applying the BM procedure to an estimated sparse concentration matrix. First the procedure can falsely select non-dominant units if the diagonal elements are very large in comparison to the off diagonal elements in a given column. The diagonal elements are the inverse of the residual variance. In combination with the LASSO estimator which minimizes the RSS, the residual variance can become relatively small making the diagonal element in the concentration matrix large in relation to the off diagonal elements. A second challenge is that the BM procedure does not take the number of non-zero elements, or connections, into account. In the

³ Alternative methods for the estimation of the concentration matrix including thresholding the sample covariance matrix are discussed in Sulaimanov and Koeppl (2016).

extreme, the BM procedure can therefore select a unit with none or a small number connections to other units. To avoid this issue, we restrict the selection in the Monte Carlo Simulation and the empirical exercise. We also assume at least one dominant driver. The advantages of the BM procedure are besides the simple implementation the robustness to common factors, something which is confirmed in our Monte Carlo Simulations.

Finally it should be noted that the sample covariance matrix can be degenerated if N > T. Bien and Tibshirani (2011) discuss this case assuming that the selected data is only a subset of the underlying data and missing units are not connected to the sample. We can ignore those units in our approach since non-connected units will have no influence on the selection of the dominant drivers. Secondly we note that the matrices $\hat{\beta}$ and $\hat{\kappa}$ are not symmetric. Meinshausen and Bühlmann (2006) ensures symmetry by using the AND criterion. Nodes i and j are connected if $\beta_{i,j} \neq 0$ and $\beta_{j,i} \neq 0$. Since we are interested in directed networks, $\hat{\beta}$ and $\hat{\kappa}$ are non-symmetric. Therefore the DDS step is restricted to the column norm.⁵

3 Monte Carlo Simulation

To show the Oracle properties of the proposed estimator, we employ a Monte Carlo Simulation. The simulations aim to shed light on three criteria: 1) model selection; that is if the individual LASSO estimators select the correct units; 2) if the number of dominant drivers is correctly estimated and 3) if the correct dominant drivers are selected. In total we are comparing 5 different specifications. Our data generating process follows Kapetanios et al. (2021):

$$\mathbf{y}_{t,d} = \mathbf{\mu}_d + \gamma_d \mathbf{g}_t + u_{d,t} ,$$
 $i = 1, ..., N_d$ (9)
 $\mathbf{y}_{t,nd} = \mu_{nd} + \beta \mathbf{y}_{t,d} + \gamma_{nd} \mathbf{g}_t + u_{nd,t} ,$ $i = N_d + 1, ..., N$ (10)

$$\mathbf{y}_{t,nd} = \mu_{nd} + \beta \mathbf{y}_{t,d} + \gamma_{nd} \mathbf{g}_t + u_{nd,t}, \qquad i = N_d + 1, ..., N$$
 (10)

where $y_{t,d}$ denotes a $N_d \times 1$ vector of the N_d dominant drivers and $y_{t,nd}$ a $N_{nd} \times 1$ vector of the N_{nd} non dominant units. The fixed effects μ_d and μ_{nd} are drawn from a uniform distribution with IIDU(0,1).

 β is a $N_d \times N_{nd}$ matrix and measures the impact of the dominant drivers on the non-dominant units and the individual elements are generated as:

$$\beta_{ij} = \begin{cases} IIDU(0,1), & \text{if } i \leq \lfloor (N - N_d)^{\alpha} \rfloor \\ 0, & \text{otherwise} \end{cases}$$

In the case of $\alpha = 1$ the dominant drivers affect all non dominant units. In the case of $\alpha < 1$, only a subset is affected by the dominant drivers, for a discussion see Kapetanios et al. (2021). The common factors f_t are uncorrelated

⁴Kapetanios et al. (2021) discuss this issue and call it the *modified BM* procedure.

⁵In a footnote BM state that the row norm can be used instead because of the symmetry of the concentration matrix.

across time and the loadings γ_d and γ_{nd} are drawn for each unit separately from a IIDU(0,1) distribution.⁶ The random noise $u_{d,t}$ and $u_{nd,t}$ are allowed to be correlated over time, measured by ρ_i and generated as a Gaussian process. The weak cross-sectional dependence in $u_{d,t}$ and $u_{nd,t}$ is measured by ρ_d and ρ_{nd} . The dependence structure over time and space is varied between the different specifications.

Specification	$ ho_d$	ρ_{nd}	$ ho_i$	α	N_d
(1)	0	0	0	1	5
(2)	0	0	0	0.5	5
(3)	0	0	IIDU(0.2,0.5)	1	5
(4)	IIDU(0.2,0.5)	0.5	0	1	5
(5)	0	0	0	1	f(N)

Table 1: Monte Carlo Specifications. N and T are varied between 50, 100 and 150. ρ_d and ρ_{nd} control the degree of cross-section dependence in the random noise $u_{d,t}$ and $u_{nd,t}$. Autocorrelation in the noise in present if $\rho_i \neq 0$. α controls the strength of the dominant units, with $\alpha = 1$ affecting all units and $\alpha = 0.5$ affecting only a share. The number of dominant drivers N_d in Specification (5) are $N_d = 0.1N$, $N_d = 0.5N$ and $N_d = 0.9N$.

Specification 1 is the simplest, with neither autocorrelation or dependence in the normally distributed (Gaussian) errors. The dominant driver affects all units. Specification 2 allows for weakly dependent dominant drivers by changing α to 0.5. Specification 3 is an alternation of specification 1 and allows for autocorrelation in the errors. Specification 4 relaxes the cross-section independence assumption of the errors. Finally, Specification 5 is the same as specification 1 but the number of dominant drivers increases with the number of cross-sections.

The number of time periods and cross-sections varies between N and T=50,100,150. The number of dominant drivers is fixed to 5 and the factors varies between 0, 1 and 5.7 We present results for the HAC robust rigorous LASSO and the adaptive LASSO.8 To select the hyperparamter λ of the adaptive LASSO we use the AIC, AICC or BIC criterion. The first stage loadings \hat{w} are calculated $\hat{w}_j = 1/abs(\hat{\beta}_j)$ where $\hat{\beta}_j$ are from an univariate OLS regression of $y_{i,t}$ on $y_{j,t}$ (Zou, 2006; Huang et al., 2008). In the first step we employ the LASSO estimators to select the non zero elements for each cross-section unit (row), then use post-LASSO OLS to estimate the coefficients of the $N \times N$ matrix β and finally construct the concentration matrix $\hat{\kappa}$ following Equation (7). We then calculate the column norms, order them by size and use the BM procedure based on Equation (8).

 $^{^6}$ For more details see Section A in the Appendix.

⁷Additional simulations with 0 and 1 dominant drivers, specifications with χ^2 distributed errors and different dependence structures are available in the online appendix.

⁸We also considered the elastic net LASSO in some preliminary simulations. Results were qualitatively worse than the adaptive or rigorous LASSO. We also acknowledge that other LASSO estimation methods such as the graphical LASSO (Friedman et al., 2008) can be employed to select the model.

To assess if the LASSO estimators select the correct dominant drivers in the individual estimations we calculate the average number of non-zero elements in each column of κ . Additionally we present the True Positive Rate (TPR), the False Positive Rate (FPR) and the False Discovery Rate (FPR) which are calculated as:

$$TPR_{N} = \frac{\sum_{i \neq j} \sum I(\hat{\kappa}_{ij} \neq 0, \text{ and } \kappa_{ij} \neq 0)}{\sum_{i \neq j} \sum I(\kappa_{ij} \neq 0)}$$

$$FPR_{N} = \frac{\sum_{i \neq j} \sum I(\hat{\kappa}_{ij} \neq 0, \text{ and } \kappa_{ij} = 0)}{\sum_{i \neq j} \sum I(\kappa_{ij} = 0)},$$

$$FDR_{N} = \frac{\sum_{i \neq j} \sum I(\hat{\kappa}_{ij} \neq 0, \text{ and } \kappa_{ij} = 0)}{\sum_{i \neq j} \sum I(\hat{\kappa}_{ij} \neq 0, \text{ and } \kappa_{ij} = 0)}.$$

$$(12)$$

$$FPR_N = \frac{\sum_{i \neq j} I(\hat{\kappa}_{ij} \neq 0, \text{ and } \kappa_{ij} = 0)}{\sum_{i \neq j} I(\kappa_{ij} = 0)},$$
(12)

$$FDR_N = \frac{\sum_{i \neq j} \sum I(\hat{\kappa}_{ij} \neq 0, \text{ and } \kappa_{ij} = 0)}{\sum_{i \neq j} \sum I(\kappa_{ij} \neq 0)}.$$
 (13)

For the dominant drivers we perform the same analysis. We present the average number of estimated dominant drivers and assess if the correct ones are selected by comparing the TPR, FPR and FDR.

The simulations are done in R for the adaptive LASSO using glmnet (Friedman et al., 2010) and repeated 1000 times. For the rigorous LASSO the Stata command rlasso (Ahrens, Hansen and Schaffer, 2020) is used with 100 repetitions.9

3.1 Results

We start with analysing the NSS step of Specification 1 with 5 dominant drivers. Table 3 shows the results for the cases with no, one and five common factors. \hat{s} is the average of non zero column norms and should be equal to $(N_d(N_d-1)+(N-N_d)N_d)/N=[4.9,4.95,4.97]$, as shown in the last block called "Oracle OLS". The rigorous and adaptive LASSO both overselect the number of non-zero elements in the β matrix. While the adaptive LASSO tends to improve with an increase in N and T, the rigorous LASSO tends to select more non zero elements. Still the true positive rate is relatively small, indicating that the rigorous LASSO misses out many non-zero elements. However this is not necessarily a disadvantage because the identification of the dominant driver relies on the column norms of the concentration matrix and thus on the size of the estimated coefficients. As long as the falsely selected non dominant drivers obtain a smaller entry in $\hat{\kappa}_{i,j}$ than the dominant drivers, the column norms of the dominant drivers will be larger than those of the non-dominant units. An advantage of the rigorous LASSO is that it falsely selects an element in the

⁹We use a correction for the Brownlees and Mesters (2021) criterion. If the criterion selects as the largest growth the last possible growth rate, we use the 2nd largest growth rate. This in particular happens if the column norm for specific units turns to zero.

concentration matrix less often than the adaptive LASSO (FPR). If the number of common factors is increased, the adaptive LASSO tends to select better than the rigorous LASSO. This can be seen by the general increase in the TPR.

Next we turn to the estimation of the dominant drivers. While the number of non-zero elements in a given column of κ gives an indication if a unit is dominant or not, the size of the post LASSO coefficient matters more. Table 4 shows the estimated number of dominant drivers and if the correct units were select for specification 1 with 5 dominant drivers. In the case of no common factors, the approach using the rigorous LASSO and adaptive LASSO, independent of the selection criterion, estimate the number of dominant drivers precisely. This is especially the case for T=150. The TPR is exactly or close to 100% implying that all dominant drivers are correctly identified. A special case for the adaptive LASSO is if N = T, in which the number of dominant drivers is underestimated. A reason for this might be the estimation of the initial loadings, which is done by OLS for each unit separately and relies on 50, respectively 100 observations.¹⁰ Noteworthy is that for small T, the rigorous LASSO underestimates the number of dominant drivers. Both, the FPR and the FDR are small and converge to zero for both LASSO estimators. For the remainder of the paper we will focus on the results from the estimation of the dominant drivers.

Next we allow the dominant drivers to be weakly dominant, meaning a dominant driver affects only a subset of the non-dominant units. We set $\alpha=0.5$, implying that only the first 6 (N=50), 9 (N=100) and 12 (N=150) non dominant units are affected. The results are displayed in Table 5. Again the adaptive LASSO underestimates the number of dominant drivers if N=T. The estimated number of dominant drivers using the rigorous LASSO is slightly downward biased as well, however the bias decreases with N and T increasing. Interestingly the rigorous LASSO improves with an increase in the number of factors, while the adaptive LASSO does much worse in comparison to Specification 1. It selects a smaller number of dominant drivers and falsely identifies non dominant drivers as such. A reason for this is that the adaptive LASSO tends to select less non-zero elements in the β matrix and therefore raises the chance to miss out dominant drivers respectively gives more weight to incorrectly selected non-dominant units. Both LASSO approaches outperform the BM criterion, even for the case of N < T.

Specification 3 allows for autocorrelated errors. Results are similar to Specification 1, however distortions when using the adaptive LASSO in the case of N=T are less pronounced. As expected, both methods control well for autocorrelation in the errors. Noteworthy is that the BM procedure performs well for the case N < T, but is affected when the number of dominant drivers is smaller than the number of common factors.

So far we assumed strong cross-section independence in the random noise. The sole source of dependence were the dominant drivers or the common factors. To relax this assumption, Specification 4, Table 7, allows for weak dependence in the random noise components. The D^2ML approach is still robust to weak

¹⁰We tested a specification with N = 50, 100, 150 and T = N - 5 and results behave better.

dependence. However the TPR for the cases with more than one dominant driver shrinks, especially for the rigorous LASSO as it underestimates the number of dominant drivers. An increase in T mitigates the problem, but the bias remains.

As a final exercise we return to specification 1 but increase the number of dominant drivers as $N_d = hN$ with h = [0.1, 0.5, 0.9]. Table 8 shows the results for $N_d = 0.1N$, implying that 10% of the cross-sections are dominant drivers. In the case of h = 0.1, all methods identify the number of dominant drivers well, but as before the adaptive LASSO underselects if the number of common factors is 5. Similarly, the rigorous LASSO does better if the number of common factors increases. Both estimator improve with an increase in T. If the share increases, it is getting harder for the estimator to identify the correct units. A reason for this is that the cut-off point in the BM criterion is less defined. This is in particular the case if h = 0.9, implying that 90% of the units are dominant ones.

In general the results show that the our proposed method reliably estimates the correct number of dominant drivers and identifies the correct drivers. In comparison to the criterion from Brownlees and Mesters (2021) our method can be applied to datasets with N>T. Both LASSO estimator have their strength and weaknesses. While the rigorous LASSO is less affected by common factors, the adaptive LASSO tends to do better in the presence of weakly correlated errors. The case of 5 common factors is interesting with respect that the method based on the rigorous LASSO identifies the correct dominant drivers and the correct number, while the adaptive LASSO performs poorly. A possible reason might again be the first stage of the adaptive LASSO and difficulties differentiating the common factors and dominant drivers.

4 Dominant Drivers in National Inflation Rates

In this section we turn back to the question if national inflation rates are exposed to dominant drivers. We use the GVAR database (Mehdi Raissi and Mohaddes, 2020) with quarterly observations from 1979Q2 to 2019Q4 (T=163) for $N_g=33$ countries. The data is in first differences, standardized and demeaned on a country level. Taking first differences is necessary to remove potential non stationary, which ensures that the covariances are not time dependent and that the post-LASSO estimates are unbiased. Standardisation is required to ensure that the coefficients from the sequential regressions of D^2ML are estimated in the same units.

There are some notable differences between our work and the literature. The years covered in the GVAR dataset are different to Ciccarelli and Mojon (2010) and more in line with Levin and Piger (2004); Rogoff (2003) who cover the years from 1980 onwards. A key difference to Ciccarelli and Mojon (2010) is that we investigate the effect of global inflation on national inflation. If a variable country combination is selected as a dominant driver, it implies that it is an important driver for the inflation rate in many countries.

We will start by applying the BM procedure to the inflation series of the

GVAR dataset. However the procedure can only be applied to a single series and dominant drivers of national inflation might be influenced by further covariates. We therefore apply the D^2ML approach afterwards which overcomes the two limitations of the BM procedure.

4.1 Number of Common Factors and BM Procedure

In a first step we estimate the number of common factors using the criteria from Bai and Ng (2002) and Ahn and Horenstein (2013). The panel criteria from Bai and Ng (2002) identifies between 4 and 5 common factors and the panel information criteria 1. Both estimator from Ahn and Horenstein (2013) point to 1 common factor. The latter results are in line with the finding in Ciccarelli and Mojon (2010) who find one common factor. In addition testing for strong cross-section dependence (Pesaran, 2015) confirms the occurrence of strong cross-section dependence.

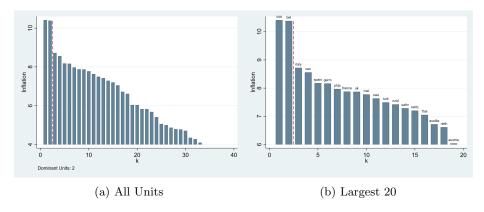


Figure 1: Column norms of the inverse of the sample covariance matrix of national inflation. Number of dominant drivers estimated by the BM procedure. See Table 11 for country name definitions and section 4 for a detailed description.

The results imply an underlying common factor structure. To shed more light if the dependence structure is driven by common factors or dominant drivers, we apply the BM procedure next. Therefore we invert the sample covariance matrix to obtain the concentration matrix. Figure 1 shows the column norms of the concentration matrix. The dotted line indicates the dominant driver identified by the BM procedure. We find that the US and Belgium are dominant drivers in the national inflation series for the 33 countries. The two dominant drivers are connected to each other and all other drivers because the concentration matrix is non-sparse. While the US is somewhat expected to be a dominant driver, the finding that Belgium is a dominant drivers is surprising. However this is in line with Ciccarelli and Mojon (2010, Table 3) who find that a large share of the detrended inflation variance of Belgium is explained by al-

ternative measures of global inflation, pointing that Belgium's inflation rate is highly connected.

A disadvantage of this approach is that the resulting concentration matrix picks up noise which can drive the determination of the dominant drivers. Secondly it is not possible to add any further covariates which might have an influence on national inflation and limiting the effects of the dominant drivers only on inflation. We therefore apply the D^2ML approach next.

4.2 Using the D^2ML approach

To allow other variables to have an effect on national inflation, we employ the D^2ML approach as described in Section 2. We model inflation as a function of inflation in foreign countries (\mathbf{dp}_{-i}) and real GDP (\mathbf{y}_i) , real equity prices (\mathbf{ep}_i) and exchange rates (\mathbf{er}_i) and the nominal short run (\mathbf{r}_i) and long run interest rate (\mathbf{lr}_i) of the domestic and foreign countries. All variables are in first differences to remove potential non stationary and standardized for each country. Standardisation is necessary to ensure that all estimated coefficients are measured in the same units. An advantage of our approach is that if a variable has no influence on the inflation rate, the LASSO estimator will set the respective coefficient and thus influence to zero. In detail, we estimate the following model:

$$\mathbf{Y}_{i,k} = \mathbf{X}_{-(i,k)} \boldsymbol{\beta}_{i,k} + \mathbf{e}_{i,k}, \quad k = 1,..,K$$
 (14)

$$\mathbf{X} = (\mathbf{dp}, \mathbf{y}, \mathbf{ep}, \mathbf{eq}, \mathbf{lr}, \mathbf{r}) \tag{15}$$

$$\tilde{\boldsymbol{\beta}}_k = \left(\boldsymbol{\beta}_{1,k}, ..., \boldsymbol{\beta}_{N,k}\right)' \tag{16}$$

$$\boldsymbol{\beta} = \left(\tilde{\boldsymbol{\beta}}_1, \dots, \tilde{\boldsymbol{\beta}}_K\right)' \tag{17}$$

where $\mathbf{Y}_{i,k}$ is the i-th element of the k-th variable of \mathbf{X} . $\mathbf{dp}, \mathbf{y}, \mathbf{dp}, \mathbf{ep}, \mathbf{eq}, \mathbf{lr}, \mathbf{r}$ are $T \times N$ matrices and $\boldsymbol{\beta}_{k,i}, k = 1, ..., 6$ are $1 \times N$. The subscript -(i,k) denotes that the i-th element in the k-th variable of X is zero. \mathbf{e}_i is a $T \times 1$ vector of random noise. $\boldsymbol{\beta}$ is a $NK \times NK$ matrix which is used to calculate the concentration matrix. $\tilde{\boldsymbol{\beta}}_k$ is a $N \times NK$ matrix with the coefficients which measure the influence on the k-th variable.

To estimate β , the following equation is estimated using the rigorous and adaptive LASSO:

$$\hat{\boldsymbol{\beta}}_{i}^{\lambda_{i}} = \arg\min_{\beta_{i}} \left(\mathbf{Y}_{i,k} - \boldsymbol{\beta}_{i} \mathbf{X}_{-(i,k)} \right)^{2} + \lambda_{i} \sum_{j=1}^{N} \psi_{i} |\boldsymbol{\beta}_{-(i,k)}|$$
(18)

The concentration matrix κ is calculated following Equation (7). Since we are only interested in the dominant drivers for inflation, that is in the first N off diagonal elements of β , we place further constraints on κ for the application

of the BM procedure. Let's denote $\hat{\beta}^c$ the constraint version of $\hat{\beta}$ and define it

$$\hat{\tilde{\beta}}^c = \begin{pmatrix} \hat{\tilde{\beta}}_1 \\ \mathbf{0} & I_{N(K-1)} \end{pmatrix}$$
 (19)

Then the estimate of the concentration matrix $\hat{\kappa}$ becomes:

$$\hat{\boldsymbol{\kappa}} = \hat{\mathbf{D}} \left(I - \hat{\tilde{\boldsymbol{\beta}}}^c \right)$$

$$\hat{\mathbf{D}} = diag(1/\hat{\sigma}_{i,k}^2)$$
(20)

$$\hat{\mathbf{D}} = diag(1/\hat{\sigma}_{ik}^2) \tag{21}$$

The lower (N-1)K rows of $\hat{\vec{\beta}}^c$ represent the effects of the covariates on all variables but inflation. Since we are only interested in inflation, this part is set to zero with the only exception of the diagonal. Non-zeros on the diagonal are required to ensure that the columns receive the equal weight for the BM procedure. The diagonal elements are the inverse of the residual variance of the regression representing the respective row. For example $\hat{\sigma}_{1,1}$ is the variance of the residuals of inflation of Argentina on the variables selected in the NSS stage by the LASSO estimators.

For the selection of the dominant drivers, we use the modified version of the BM procedure. The selection is restricted to the N/2 most connected units (Kapetanios et al., 2021). This has the advantage that we filter out units with very large values on the diagonal, but without any connection to other units.

4.2.1 No Common Factors

Rigorous LASSO First we employ the rigorous LASSO on Equation (18) which allows for heteroskedasticity and autocorrelation of order 2.¹¹ Column (1) in Table (2) displays the results. We identify the inflation series of the US as the strongest and of Belgium as the second dominant drivers. Together the dominant drivers account for 57.58% of the column norms and they influence in total 15 other units. 12 D^2ML identifies 26 connections between units of which 13 are related to the two dominant drivers. Important to note is that the inflation rate in the US influences the inflation rate of 8 other countries, while the Belgium inflation rate influences 5 others.

An alternative method to display the results is to look at the column norms directly. Panel (a) of Figure 2 shows the column norms across all country and variable combinations, Panel (b) only the largest 20. Each bar represents a country and a variable. For example the largest bar in Figure 2 is the column norm of the US inflation. All country-variable combinations to the left of the

¹¹We varied the bandwidth between 0, 1, 2, 4, and 8, to cover autocorrelation over several quarters. The results remain unchanged and are presented in the Online Appendix.

¹²Diagonal elements are not counted in the column norm shares or the number of non-zero

	ٺ	1)	_	(5)	ت	(3)	(4)	
		Rigorous LASSO	Γ			Adaptive LASSO	LASSO	
Common Factors		No		Yes		No		Yes
Number of dom. Units —								
1	dp(bel)	2	dp(bel)	5	r(chl)	2	r(chl)	5
		(27.38%)		(29.16%)		(23.90%)		(28.65%)
2	dp(usa)	∞	dp(usa)	7	dp(usa)	10	dp(usa)	10
		(30.19%)		(27.71%)		(19.64%)		(23.10%)
3			poil	∞				
				(20.29%)				
Share columnorms of dom. units.	om. units.							
		57.58%		77.17%		43.54%		51.76%
No. Connections								
Dominant		13		20		15		15
Total		26		26		38		33

Table 2: Column norms of estimated concentration matrix based on Equation (20). The diagonal elements for calculation of dp() denotes national inflation rates, r() national short run interest rates and poil oil prices. Abbreviations for countries are column norm shares and number of connections are removed. Column norm shares for dominant drivers are in parenthesis. United States (USA), Belgium (bel) and Chile (chl). See Table 11 for country name definitions and section 4 for a detailed description. Then penalty factor is selected by the BIC criterion for the adapative LASSO.

dashed red line are dominant drivers.

Panel (a) shows the distribution of all column norms. We note that inflation has six non-zero column norms, real GDP and real equity prices have one non-zero column norm each. In Panel (b) it becomes evident that the growth rate from the US to the German interest rate is largest and therefore marks the border between dominant and non dominant units.

The lower panel of the figure displays a network graph of the dominant drivers. It is noteworthy that the US influences Belgium but not the other way around. Belgium is a dominant driver for only European countries, while the US influences most of western Europe and Japan and Canada. The effect of Belgium is somewhat surprising. Besides the explanation discussed in the previous section, it is possible that the influence of Eurozone inflation on the national inflation rates not only within the Eurozone but outside of it are picked up by the Belgium inflation. Our finding is in line with argument in Bataa et al. (2013) that national inflation in Eurozone countries moves together and Belgium is a proxy for it. Further it extends the finding in Billio et al. (2016) that US leads the Eurozone cycle to inflation.

Adaptive LASSO Next we employ the adaptive LASSO as the selection method of the NSS stage.¹³ The adaptive weights origin from a univariate regression, similar to the Monte Carlo simulation. The penalty loading is selected using the BIC criterion.

The third column in Table 2 shows the results for this approach. Two dominant drivers are identified, the short run interest rate in Chile and as in the case of the rigorous LASSO the inflation rate in the US. While the US influences a larger number of drivers, the influence of the Chilean short run interest rate is stronger. The number of identified connections is much larger than in the case of the rigorous LASSO. Figure 3 shows that the inflation series are again picked up most often influencing other inflation series. Panel (b) shows that inflation in Belgium is again influencing strongly other inflation rates, but it is not picked as a dominant driver.

Turning to the network graph in Figure 3 it becomes evident that the short run rate in Chile not only influences the inflation rate in Chile but other countries as well. Among the main drivers for the column norm of the short run rate of Chile is however the affect on the inflation in Chile. The US has a similar widespread influence on inflation rates again. Together with the short run rate of Chile, the two dominant drivers influence 15 out of the 38 national inflation series.

Our results are in contrast to Ciccarelli and Mojon (2010) who find that no country is leading global inflation. Our results strongly suggest that the United

 $^{^{13}\}mathrm{We}$ further restrict the selection of the dominant drivers such that the diagonal is less than 50% of the absolute sum.

States are a dominant factor for national inflation. Depending on the model selection method, Belgium respectively the short run interest rate in Chile are selected as dominant drivers.

4.2.2 Observed Common Factors

It is likely that inflation is not only driven by specific countries, but by other global factors. Examples would be commodity prices, see Aastveit et al. (2015). To investigate the effect of such observed common factors, we add the prices of oil (p_{oil}) , metals (p_{met}) and materials (p_{mat}) to the set of variables in matrix \mathbf{X} in Equation (15):

$$X = (dp, y, ep, eq, lr, r, p)$$
(22)

$$\mathbf{p} = (\mathbf{p}_{oil}, \mathbf{p}_{mat}, \mathbf{p}_{met}) \tag{23}$$

The commodity prices are the same across the 33 countries and they are allowed to be selected as a dominant driver. Results are presented in column (2) and (4) of Table 2 and in Figure 4. A comparison between Column (3) and (4) reveals that the adaptive LASSO is not influenced by the additional observed common factors and the results remain similar. We therefore turn directly to the rigorous LASSO. Again the US and Belgium are selected as dominant drivers, however oil prices are selected as a third a dominant driver. In fact, they account for 20.3% of the column norms. The network structure of the two other drivers remains almost unchanged. The US is not directly connected to Switzerland any longer but the shares of the column norm remain stable. As shown in the Monte Carlo simulation, not accounting for common factors does not worsen the identification of dominant drivers using the rigorous LASSO as a selection method.

The network graph in Figure 4 reveals that inflation in Austria, Finland, France, Italy, Switzerland and Thailand is influenced by the global oil prices. Oil prices are also influencing the two other dominant drivers, Belgium and the US, emphasising further their importance.

Our results so far show that the US and oil prices play a crucial role for national inflation rates. In line with the results in Ciccarelli and Mojon (2010) is that some countries are sheltered from the dominant drivers. Our analysis shows that the inflation hardly spills over into countries such as China, India or Norway. Implying that for those countries other factors than the ones covered in our empirical application play an important role in determining national inflation.

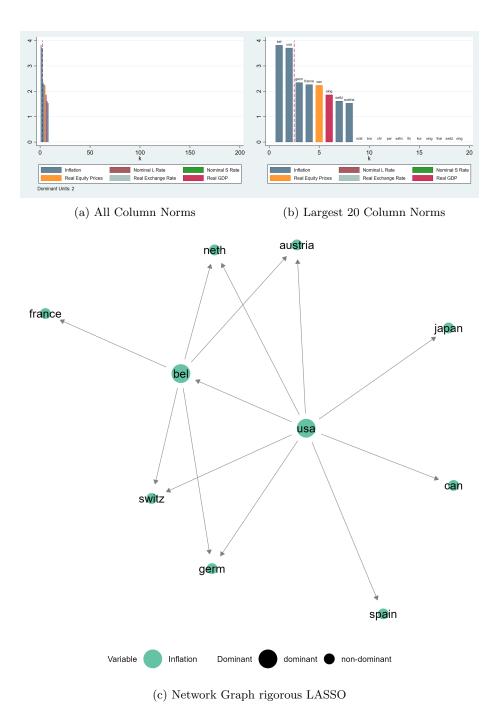


Figure 2: Column Norms and Network Graph for dominant drivers using rigorous LASSO in the NSS step. Norms to the left of the red dotted line are dominant drivers in Panel (a) and (b). See Table 11 for country name definitions and section 4 for a detailed description.

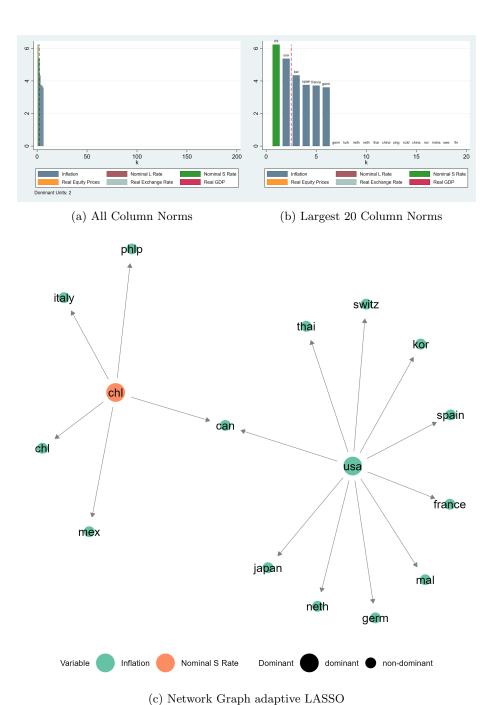
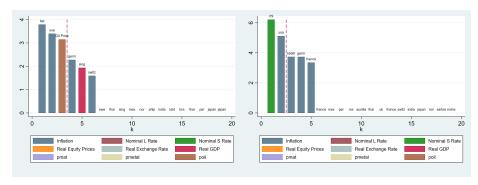
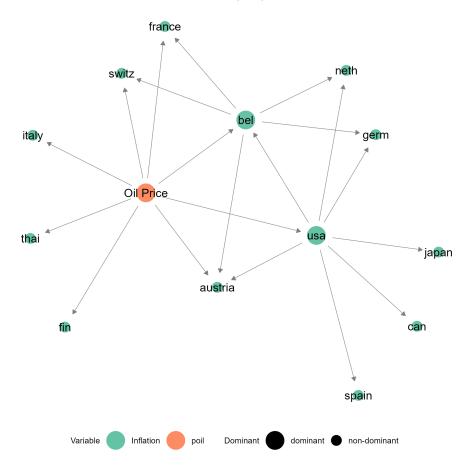


Figure 3: Column Norms and Network Graph for dominant drivers using adaptive LASSO in the NSS step. Then penalty factor is selected by the BIC criterion. Univariate OLS is used in the calculation of the weights. Norms to the left of the red dotted line are dominant drivers in Panel (a) and (b). See Table 11 for country name definitions and section 4 for a detailed description. $19\,$



(a) Column Norms from Rigorous LASSO (b) Column Norms from Adaptive LASSO (BIC)



(c) Network Graph Rigorous LASSO

Figure 4: Commodity prices added as covariates. Column Norms for the rigorous and adaptive LASSO. Norms to the left of the red dotted line are dominant drivers in Panel (a) and (b). See Table 11 for country name definitions, section 4 for a detailed description and note from

Figures 2 and 3.

4.3 Unobserved Common Factors

We further account for unobserved common factors.¹⁴ We approximate potential unobserved common factors using principal components (PCA) or cross-section averages. Both methods are well established in the literature to account for unobserved common factors (Pesaran, 2006; Bai, 2009). In the previous section we found up to 4 common factors. Assuming that some of those are dominant drivers, we add the first 3 principal components (PCA). Separately the cross-section averages (CSA) of all variables are added to the model. The PCA and CSA are added in the same way as the observed common factors in the previous section.

The findings are similar to the case of adding observed common factors. Using thee adaptive LASSO we identify Chile as the sole dominant drivers. The rigorous LASSO only identifies the first principal component respectively the cross-section average of inflation as a dominant driver. This implies that the approximation of the unobserved common factors accounts for too much of the variation and overlays the network structure. The result hints that the strong dependence of the common factor overlays weaker dependence structure, a similar finding as in Juodis (2022). Furthermore the long run interest rate in Germany is selected as a dominant driver and it influences the inflation rate in Switzerland and the United Kingdom.

5 Conclusion

This paper combines the approach by Meinshausen and Bühlmann (2006); Sulaimanov and Koeppl (2016) to estimate the inverse of a covariance matrix using time dependent data. It then identifies dominant drivers using the procedure from Brownlees and Mesters (2021). Monte Carlo simulations show that D^2ML identifies the correct units as dominant drivers in a panel. We then apply the method to the GVAR dataset and find evidence that inflation in the US and oil prices are dominant factors for national inflation rates. Our results are informative about potential spillovers into national inflation. It can also be used to improve forecasts using an approach as in Bjørnland et al. (2017).

While D^2ML is simple, it has several limitations. First of all it is computationally expensive, in particular for a large number of cross-sections, respectively variables. Secondly as criticized by Yuan and Lin (2007); Banerjee et al. (2008); Friedman et al. (2008) the approach by Meinshausen and Bühlmann (2006) is only an approximation to the problem. An extension in the spirit of this paper would be to use graphical LASSO (Friedman et al., 2008) for time dependent data. The selection of an oracle estimator for the NSS step is crucial. If the selected estimator fails, the sequential estimator will fail as well. In our current setting higher order spatial effects and time varying dominant drivers are also not be considered and left for future research.

¹⁴Detailed results are available in the Online Appendix.

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A Detailed Monte Carlo Settings

The loadings of the common factors f_t are generated as:

$$\begin{split} \boldsymbol{\gamma}_{d} &= (\gamma_{1},..,\gamma_{N_{d}}) \\ \boldsymbol{\gamma}_{nd} &= (\gamma_{N_{d}+1},..,\gamma_{N}) \\ \gamma_{i} &\sim IIDU(0,1), \ i=1,...,N \end{split}$$

The unobserved common factors are generated as

$$\begin{aligned} \boldsymbol{g}_t &= \boldsymbol{R}_g^{1/2} \left(g_t - 2\tau_k \right) / 2 \\ g_t &\sim IID\chi^2(2) \\ \boldsymbol{R}_g &= \left(1 - \rho_g \right) \boldsymbol{I}_{m_k} + \rho_g \tau_k \tau_k' \\ \rho_g &= IIDU(0.2, 0.8) \end{aligned}$$

with $\tau_k = (1, ..., 1)'$.

The random noise $u_{d,t}$ and $u_{nd,t}$ are allowed to be correlated over time and generated as a Gaussian process:

$$\begin{aligned} \boldsymbol{u}_{d,t} &= \left(1 - \rho_i\right) \boldsymbol{R}_d^{1/2} \left(\boldsymbol{u} *_{d,t} - 2\tau_{N_d}\right) / 2 + \rho_i \boldsymbol{u}_{d,t-1} \\ \boldsymbol{R}_d &= \left(1 - \rho_d\right) \boldsymbol{I}_{N_d} + \rho_d \tau_{N_d} \tau_{N_d}' \\ \boldsymbol{u} *_{d,t} &\sim IIDN(0,1) \end{aligned}$$

and for the non dominant drivers:

$$\begin{split} u_{nd,it} &= \rho_i u_{nd,it-1} + \left(1 - \rho_i^2\right)^{1/2} \epsilon_{it} \\ \epsilon_t &= (\epsilon_{N_{nd}t}, \dots, \epsilon_{Nt}) = \Sigma^{1/2} \boldsymbol{R}_{nd}^{1/2} \boldsymbol{\xi}_t \\ \Sigma &= diag\left(\sigma_1 1, \dots, \sigma_{NN}\right) \\ \sigma_{ii} &= IID\chi^2(2)/4 + 0.5 \\ \boldsymbol{\xi}_t &= IIDN(0,1) \\ \boldsymbol{R} &= \begin{pmatrix} 1 & \rho_{nd} & \rho_{nd}^2 & \dots & \rho_{nd}^{n_{nd}-1} \\ \rho_{nd} & 1 & \rho_{nd} & \dots & \rho_{nd}^{n_{nd}-2} \\ \vdots & & & \vdots \\ \rho_{nd}^{n_{nd}-1} & \rho_{nd}^{n_{nd}-2} & \rho_{nd}^{n_{nd}-3} & \dots & 1 \end{pmatrix} \end{split}$$

B Monte Carlo Results

N/T		$\frac{\hat{s}}{100}$	150	50	TPR 100	150		FPR 100	150	50	FDR 100	150
	ber of Fact		100	30	100	100	30	100	100	50	100	150
50	ous LASSO 46.08	51.73	55.29	15.37	25.59	30.81	8.25	11.57	13.35	35.05	31.10	30.24
100	88.66	97.51	104.38	9.25	17.20	22.83	4.80	6.91	8.27	34.31	28.62	26.62
150	138.84	145.65	155.11	7.50	13.52	18.61	3.93	5.16	6.54	34.39	27.47	26.03
Adap	otive LASS	O (AIC)										
50	47.50	18.82	15.87	97.47	73.57	76.26	94.75	34.08	27.33	49.29	31.61	26.35
100	39.95	96.88	48.42	57.66	97.02	79.89	39.12	96.88	46.85	40.46	49.96	36.94
150	42.79 otive LASS	68.41 O (AICC)	146.27	49.03	58.35	96.56	27.93	45.18	97.55	36.36	43.65	50.25
$\frac{Adap}{50}$	26.15	11.29	12.04	69.39	66.23	73.02	50.62	18.26	19.24	41.82	21.63	20.85
100	7.63	36.35	16.64	35.19	61.93	69.12	6.25	35.07	14.03	15.17	35.69	16.90
150	10.44	10.29	41.89	32.54	41.31	59.00	6.13	5.71	26.90	15.91	12.20	30.93
	otive LASS											
50	37.89	5.97	6.26	82.13	50.64	59.51	75.15	8.12	7.87	47.72	13.86	11.70
100	15.98	45.92	6.48	39.02	63.81	55.45	14.85	45.02	4.04	27.51	40.99	6.82
150 Orac	29.00 le OLS	5.19	30.76	42.05	37.06	52.93	18.88	2.34	19.43	30.99	6.00	26.38
50	4.90	4.90	4.90	100.00	100.00	100.00	0.00	0.00	0.00	0.00	0.00	0.00
100	4.95	4.95	4.95	100.00	100.00	100.00	0.00	0.00	0.00	0.00	0.00	0.00
150	4.97	4.97	4.97	100.00	100.00	100.00	0.00	0.00	0.00	0.00	0.00	0.00
	ber of Fact											
	ous Lasso (
50	56.47	59.64	62.30	13.90	21.08	25.80	15.02	19.72	23.01	52.44	48.64	47.36
100	111.73	116.91	120.90	9.04	14.13	18.32	8.97	12.05	14.29	50.17	46.36	44.06
150	167.74 otive LASS	174.48 O (AIC)	178.21	7.02	11.29	14.55	6.47	9.00	10.55	48.30	44.66	42.20
$\frac{Ada_1}{50}$	47.28	18.81	16.12	98.25	72.03	73.34	94.20	34.21	28.17	48.95	32.16	27.74
100	24.42	96.12	48.11	63.02	98.48	78.07	22.54	96.00	46.61	26.06	49.36	37.36
150	28.28	29.57	144.64	56.98	65.58	98.33	17.97	18.18	96.36	24.07	21.50	49.49
	otive LASS											
50	31.70	11.57	12.51	88.35	65.54	70.56	60.93	18.94	20.52	40.04	22.47	22.55
100 150	$7.48 \\ 7.99$	32.58 10.87	17.34 27.38	63.69 60.75	80.47 69.39	66.82	$\frac{4.68}{3.49}$	$30.19 \\ 5.18$	14.87 16.32	$7.27 \\ 5.86$	$\frac{26.00}{7.26}$	18.23 16.91
	otive LASS		21.30	00.75	09.39	76.41	3.49	5.16	10.32	3.80	1.20	10.91
50	33.99	7.38	7.56	89.10	59.43	64.52	65.89	10.33	10.24	42.04	14.91	13.77
100	7.90	20.62	8.38	64.87	80.84	61.95	5.06	17.62	5.71	7.79	17.24	8.52
150	9.77	6.38	9.58	62.29	75.84	80.37	4.85	1.87	3.92	7.88	2.59	4.90
	le OLS											
50	4.90	4.90	4.90	100.00	100.00	100.00	0.00	0.00	0.00	0.00	0.00	0.00
$\frac{100}{150}$	$4.95 \\ 4.97$	$4.95 \\ 4.97$	$4.95 \\ 4.97$	100.00 100.00	100.00 100.00	100.00 100.00	$0.00 \\ 0.00$	$0.00 \\ 0.00$	$0.00 \\ 0.00$	$0.00 \\ 0.00$	$0.00 \\ 0.00$	$0.00 \\ 0.00$
	ber of Fact		4.91	100.00	100.00	100.00	0.00	0.00	0.00	0.00	0.00	0.00
	ous Lasso (o+)									
50	68.33	71.25	72.83	30.42	38.10	42.27	19.56	24.92	28.34	39.28	39.62	40.18
100	134.52	139.41	142.65	23.29	30.23	34.33	11.78	15.30	17.64	33.70	33.68	33.99
150	198.68	206.49	211.56	19.89	26.69	31.06	8.62	11.32	13.18	30.32	29.85	29.85
	otive LASS	/										
50	7.58	6.88	6.32	92.77	65.51	67.93	7.48	8.64	7.17	7.23	11.26	9.26
100	4.03	7.71	8.60	80.84	$96.02 \\ 82.76$	68.01	0.20	3.30	5.63	0.24	3.27	7.34
150	4.02 otive LASS	4.14 (AICC)	7.67	80.43	82.70	97.02	0.09	0.10	2.05	0.12	0.12	2.06
50	5.62	6.28	6.08	92.44	64.50	67.54	3.22	7.42	6.69	3.36	10.11	8.80
100	4.01	6.32	7.54	80.51	96.06	67.09	0.19	1.84	4.57	0.24	1.88	6.25
150	4.00	4.14	6.58	80.08	82.66	97.10	0.09	0.10	1.30	0.11	0.12	1.32
	otive LASS											
50	5.52	5.33	5.27	91.73	62.42	65.90	3.07	5.54	5.06	3.23	8.10	7.04
100 150	$\frac{3.96}{3.95}$	$5.62 \\ 4.09$	$6.04 \\ 5.69$	79.58 79.11	95.93 81.74	65.36 97.22	$0.19 \\ 0.09$	$\frac{1.12}{0.09}$	$\frac{3.08}{0.68}$	$0.23 \\ 0.11$	$\frac{1.15}{0.12}$	$\frac{4.47}{0.69}$
	le OLS	4.03	0.08	10.11	01.74	31.44	0.09	0.09	0.00	0.11	0.12	0.09
50	4.90	4.90	4.90	100.00	100.00	100.00	0.00	0.00	0.00	0.00	0.00	0.00
100	4.95	4.95	4.95	100.00	100.00	100.00	0.00	0.00	0.00	0.00	0.00	0.00
150	4.97	4.97	4.97	100.00	100.00	100.00	0.00	0.00	0.00	0.00	0.00	0.00

Table 3: Monte Carlo Results for NSS and Specification 1. The number of dominant Units is set to 5. The parametrisation is summarised in Table 1. The estimated equations are (9) and (10). The initial stage for the adaptive LASSO is a univariate OLS regression if N > T and multivariate if N < T.

		»Ŷ			mp.p.			EDD			PDD	
N/T	50	$\frac{N_d}{100}$	150	50	TPR 100	150	50	FPR 100	150	50	FDR 100	150
	ber of Fa		150	- 30	100	100	30	100	100	30	100	
	ous Lass		obust)									
50	3.28	4.58	4.93	63.80	91.40	98.18	0.20	0.02	0.04	0.21	0.03	0.04
100	3.32	4.65	4.99	62.80	92.80	99.80	0.19	0.02	0.00	0.35	0.01	0.00
150	3.38	4.73	4.95	66.60	94.40	99.00	0.03	0.01	0.00	0.04	0.01	0.00
Adaj	ptive Las	so (AIC)										
50	2.50	4.99	5.00	42.24	99.68	100.00	0.87	0.01	0.00	1.59	0.01	0.00
100	$4.88 \\ 4.60$	2.51	5.00	96.40	47.80	99.96 54.20	0.06	0.13	0.00	0.07	0.96	0.00
150	ptive Las	5.00	2.76	89.40	99.92	34.20	0.09	0.00	0.04	0.16	0.00	0.24
50	2.67	5.00	5.00	40.88	100.00	100.00	1.39	0.00	0.00	2.43	0.00	0.00
100	4.98	2.39	5.00	98.64	43.76	100.00	0.05	0.21	0.00	0.05	1.32	0.00
150	4.75	5.00	2.54	94.80	100.00	48.88	0.01	0.00	0.07	0.01	0.00	0.54
Adaj	ptive Las	so (BIC)										
50	2.58	5.00	5.00	42.68	100.00	100.00	0.98	0.00	0.00	1.66	0.00	0.00
100	4.96	2.78	5.00	99.00	53.16	100.00	0.01	0.13	0.00	0.01	0.18	0.00
150	4.74	5.00	4.24	92.68	100.00	84.52	0.07	0.00	0.01	0.15	0.00	0.01
$\frac{\text{Brov}}{50}$	vnlees an	d Mesters 5.00	5.00	99.04	100.00	100.00	0.02	0.00	0.00	0.02	0.00	0.00
100	4.90	5.00	5.00	99.04	100.00	100.00	0.02	0.00	0.00	0.02	0.00	0.00
150			5.00			100.00			0.00	· ·		0.00
Num	ber of Fa	ctors: 1										
rigor	ous Lass	o (HAC r	obust)									
50	2.78	4.06	4.33	54.63	80.80	86.60	0.11	0.04	0.00	0.16	0.04	0.00
100	3.16	4.21	4.74	62.40	84.20	94.80	0.04	0.00	0.00	0.05	0.00	0.00
150	3.24	4.49	4.71	64.20	89.60	94.20	0.02	0.01	0.00	0.02	0.01	0.00
	ptive Las			44.40	00.00	100.00	1.00	0.01	0.00	2.50	0.01	
$\frac{50}{100}$	$\frac{2.53}{4.71}$	$4.96 \\ 2.65$	$5.00 \\ 4.99$	41.12 94.12	99.20 49.44	100.00 99.80	1.06	$0.01 \\ 0.19$	0.00	2.58	$0.01 \\ 0.27$	$0.00 \\ 0.00$
150	$\frac{4.71}{4.72}$	4.91	$\frac{4.99}{3.17}$	94.12	98.12	62.80	$0.00 \\ 0.01$	0.19	$0.00 \\ 0.02$	$0.00 \\ 0.01$	0.27	0.00
	ptive Las			94.32	90.12	02.00	0.01	0.00	0.02	0.01	0.00	0.02
50	2.64	4.99	5.00	41.20	99.76	100.00	1.30	0.00	0.00	3.04	0.00	0.00
100	4.83	3.26	5.00	96.52	59.04	100.00	0.01	0.32	0.00	0.01	1.02	0.00
150	4.80	4.95	3.77	96.04	99.00	74.88	0.00	0.00	0.02	0.00	0.00	0.04
	ptive Las											
50	2.69	5.00	5.00	47.24	99.92	100.00	0.73	0.00	0.00	1.69	0.00	0.00
100	4.76	4.40	5.00	95.12	87.80	100.00	0.01	0.01	0.00	0.01	0.01	0.00
150 DM	4.73 procedure	4.89	4.88	94.52	97.84	97.60	0.00	0.00	0.00	0.00	0.00	0.00
$\frac{BM}{50}$	4.54	4.73	4.81	90.44	94.56	96.08	0.04	0.01	0.01	0.04	0.01	0.01
100	4.04	4.40	4.51		87.48	89.84	0.04	0.01	0.01	0.04	0.01	0.01
150			4.27			85.24	•		0.01			0.01
Num	ber of Fa	ctors: 5										
rigor	ous Lass	o (HAC r	obust)									
50	4.77	4.97	5.00	94.80	99.40	100.00	0.07	0.00	0.00	0.07	0.00	0.00
100	4.90	4.98	5.00	97.00	99.60	100.00	0.05	0.00	0.00	0.05	0.00	0.00
150	4.77	4.98	5.00	94.80	99.60	100.00	0.02	0.00	0.00	0.02	0.00	0.00
	ptive Las			00.00	00.00	100.00	0.11	0.00	0.00	0.11	0.00	0.00
50	5.05	5.00	5.00	99.92	99.92	100.00	0.11	0.00	0.00	0.11	0.00	0.00
$\frac{100}{150}$	$3.96 \\ 4.10$	$\frac{5.15}{4.08}$	$5.00 \\ 5.22$	$78.92 \\ 81.24$	$100.00 \\ 81.12$	100.00 100.00	$0.01 \\ 0.03$	$0.16 \\ 0.02$	$0.00 \\ 0.15$	$0.01 \\ 0.03$	$0.15 \\ 0.02$	$0.00 \\ 0.15$
	ptive Las			01.24	01.14	100.00	0.00	0.02	0.10	0.00	0.02	0.10
50	5.05	5.00	5.00	99.92	99.96	100.00	0.12	0.00	0.00	0.12	0.00	0.00
100	3.92	5.17	5.00	78.24	100.00	100.00	0.01	0.17	0.00	0.01	0.17	0.00
150	4.05	4.08	5.21	80.44	81.00	100.00	0.02	0.02	0.15	0.02	0.02	0.15
	ptive Las											
50	5.04	5.00	5.00	99.92	99.92	100.00	0.10	0.00	0.00	0.10	0.00	0.00
100	3.81	5.11	5.00	76.04	100.00	100.00	0.01	0.11	0.00	0.01	0.11	0.00
$\frac{150}{\text{DM}}$	3.97	3.97	5.20	78.84	78.96	100.00	0.02	0.01	0.14	0.02	0.01	0.14
$\frac{\mathrm{BM}}{50}$	procedur 4.75	4.83	4.70	95.00	96.20	93.88	0.00	0.04	0.02	0.00	0.03	0.02
100	4.75	$\frac{4.85}{4.85}$	$\frac{4.70}{4.85}$	<i>9</i> 0.00	96.48	96.60	0.00	0.04 0.03	0.02	0.00	0.03	0.02
150			4.78			94.80			0.03			0.03
	•	•		-	•			-		-	•	

Table 4: Monte Carlo Results for estimation of Dominant Drivers, Specification 1. The number of dominant Units is 5_{27} See notes of Table 3. *BM procedure* is the procedure in Brownlees and Mesters (2021) directly applied to the inverse of the simulated sample covariance matrix.

		$\hat{N_d}$			TPR			FPR			FDR	
N/T	50	$\frac{N_d}{100}$	150	50	100	150	50	100	150	50	100	150
	ber of Fa											
		SO (HAC	robust)									
50	3.14	2.90	3.48	48.40	55.60	66.80	1.60	0.27	0.31	2.51	0.50	0.29
100	2.20	3.06	2.82	41.20	57.20	55.60	0.15	0.21	0.04	0.29	0.22	0.07
150	2.88	2.90	3.18	54.00	57.20	63.60	0.12	0.03	0.00	0.15	0.05	0.00
$\frac{\text{Adap}}{50}$	2.95	SSO (AIO 4.04	4.58	33.76	79.84	91.08	2.81	0.11	0.05	9.19	0.11	0.05
100	4.44	2.55	4.32	88.00	34.80	85.20	0.04	0.11	0.06	0.06	5.65	0.06
150	4.46	4.95	2.39	76.24	99.00	36.92	0.44	0.00	0.37	2.00	0.00	2.46
		SSO (AIC										
50	3.01	4.20	4.63	33.20	82.88	91.56	3.00	0.12	0.11	10.56	0.12	0.10
$\frac{100}{150}$	$4.24 \\ 4.40$	$\frac{2.91}{4.97}$	$4.76 \\ 2.46$	83.60 80.80	34.04 99.36	94.68 38.80	$0.07 \\ 0.25$	$\frac{1.28}{0.00}$	$0.03 \\ 0.36$	$0.28 \\ 1.11$	8.30 0.00	$0.03 \\ 3.87$
		SSO (BIO		80.80	33.30	30.00	0.20	0.00	0.30	1.11	0.00	3.01
50	3.03	4.36	4.66	33.72	83.28	89.44	2.98	0.43	0.43	9.08	0.40	0.40
100	4.35	2.48	4.83	86.16	35.44	95.76	0.05	0.74	0.05	0.09	5.35	0.05
150	4.47	4.83	2.39	79.72	96.20	43.12	0.33	0.01	0.16	1.82	0.01	1.46
$\frac{\mathrm{BM}}{50}$	procedur 4.83		5.00	05.79	99.84	100.00	0.00	0.00	0.00	0.09	0.00	0.00
100	4.83	$4.99 \\ 4.97$	$5.00 \\ 5.00$	95.72	99.84	100.00 100.00	0.09	0.00	$0.00 \\ 0.00$	0.09	0.00	0.00
150			5.00			99.96			0.00			0.00
Num	ber of Fa											
rigor	ous LAS	SO (HAC	robust)									
50	4.56	2.82	4.76	45.20	42.00	53.20	5.11	1.60	4.67	9.96	2.13	5.79
100	3.94	2.90	2.60	36.00	46.00	51.20	2.25	0.63	0.04	6.41	2.92	0.05
150	2.14	2.78 SSO (AIO	3.36	32.80	46.40	64.00	0.34	0.32	0.11	2.71	0.50	0.13
50	2.63	3.88	4.54	31.80	75.64	89.76	2.32	0.22	0.12	8.38	0.23	0.11
100	3.95	2.53	3.97	78.04	33.00	78.36	0.05	0.93	0.05	0.05	6.76	0.05
150	4.24	4.64	2.35	72.48	92.64	36.12	0.42	0.01	0.37	2.34	0.01	3.49
		SSO (AIC		00.00	00.00	00.00	0.00	0.00	0.00	11.00	0.04	
50 100	$3.15 \\ 4.51$	$\frac{4.15}{2.56}$	4.49 4.62	$32.96 \\ 87.96$	80.96 32.64	88.96 91.96	$3.33 \\ 0.12$	$0.23 \\ 0.98$	$0.09 \\ 0.03$	$\frac{11.06}{0.12}$	$0.24 \\ 7.07$	0.09
150	4.48	4.96	2.60	85.36	99.20	39.80	0.12	0.98	0.03 0.42	0.12	0.00	4.91
		SSO (BIO		00.00	00.20	00.00	0.10	0.00	0.12	0.00	0.00	
50	2.76	3.67	4.00	32.80	71.36	78.52	2.48	0.23	0.16	8.63	0.22	0.16
100	4.19	2.29	4.27	82.88	36.68	83.60	0.05	0.48	0.09	0.05	3.23	0.09
150	4.35	4.09	3.17	79.44	81.28	61.12	0.26	0.02	0.08	1.62	0.02	0.29
$\frac{BM}{50}$	procedur 2.69	e 2.89	3.08	50.68	57.24	61.60	0.36	0.07	0.01	1.07	0.28	0.01
100	2.09	$\frac{2.89}{2.49}$	$\frac{3.08}{2.56}$		49.24	50.68		0.07	0.01	1.07	0.28	$0.01 \\ 0.47$
150			2.46			48.00			0.04			0.84
Num	ber of Fa	actors: 5										
		SO (HAC										
50	3.38	4.28	4.54	66.00	85.20	90.40	0.18	0.04	0.04	0.20	0.04	0.04
$\frac{100}{150}$	$\frac{3.02}{3.60}$	$\frac{4.62}{4.38}$	$\frac{4.82}{4.88}$	59.60 70.00	91.60 87.20	96.00 97.60	$0.04 \\ 0.07$	$0.04 \\ 0.01$	$0.02 \\ 0.00$	$0.05 \\ 0.07$	$0.04 \\ 0.01$	$0.02 \\ 0.00$
		4.38 SSO (AIC		70.00	01.20	91.00	0.07	0.01	0.00	0.07	0.01	0.00
50	2.92	3.44	3.82	40.56	67.44	75.64	1.98	0.14	0.08	5.02	0.15	0.08
100	3.22	2.35	3.58	26.76	40.44	70.76	1.98	0.34	0.04	10.46	1.99	0.04
150	4.52	3.04	2.47	22.48	30.68	46.00	2.34	1.04	0.12	16.97	5.43	0.16
		SSO (AIC		26 40	CO 44	75.00	1.90	0.07	0.00	1.01	0.07	0.00
$\frac{50}{100}$	$\frac{2.44}{3.87}$	$\frac{3.54}{1.96}$	$3.82 \\ 4.21$	$36.48 \\ 26.80$	68.44 34.52	75.92 83.12	$\frac{1.38}{2.66}$	$0.27 \\ 0.25$	$0.06 \\ 0.06$	$1.91 \\ 13.65$	$0.27 \\ 1.18$	$0.06 \\ 0.06$
150	4.46	3.05	2.12	$\frac{20.80}{22.12}$	28.92	33.12	$\frac{2.00}{2.31}$	1.11	0.32	18.93	6.88	1.20
		SSO (BIO										
50	2.47	3.90	3.99	35.72	76.04	78.80	1.52	0.21	0.11	2.40	0.21	0.10
100	3.64	2.82	4.48	26.12	31.96	88.44	2.46	1.28	0.06	12.48	2.82	0.06
150 DM	4.61	3.91	2.94	22.20	26.40	30.72	2.42	1.78	0.97	17.68	9.14	3.59
BM 1	procedur 2.63	e 2.49	2.53	8.08	6.96	6.48	4.95	4.75	4.91	76.20	76.80	79.51
100	2.03	$\frac{2.49}{2.32}$	$\frac{2.33}{2.26}$	0.00	$\frac{0.90}{2.52}$	3.12	4.90	2.31	$\frac{4.91}{2.22}$	70.20	90.61	87.57
150			2.42			1.76		2.01	1.61			92.50

Table 5: Monte Carlo Results for estimation of Dominant Drivers, Specification 2. The number of dominant Units is 52%ee notes of Table 3 and Table 4.

					mp.p.							
N/T	50	$\frac{N_d}{100}$	150	50	TPR 100	150	50	FPR 100	150	50	FDR 100	150
	ber of Fa		100	30	100	100	30	100	100	- 30	100	
	ous LAS		1h									
50	3.54	$\frac{4.52}{4.52}$	5.00	60.40	90.00	99.60	1.16	0.04	0.04	1.36	0.04	0.04
100	$\frac{3.54}{2.94}$	4.32 4.36	4.96	57.20	87.20	99.20	0.08	0.04	0.04	0.12	0.04	0.04
150	3.54	4.84	4.98	64.40	96.80	99.60	0.22	0.00	0.00	0.23	0.00	0.00
Adar	otive LAS	SSO (AIC	C)									
50	2.72	4.99	5.00	50.40	99.76	100.00	0.45	0.01	0.00	0.48	0.01	0.00
100	4.99	3.26	5.00	99.88	64.68	99.96	0.00	0.03	0.00	0.00	0.04	0.00
150	4.96	5.00	4.09	99.16	100.00	81.44	0.00	0.00	0.01	0.01	0.00	0.01
	ptive LAS											
50	2.81	5.00	5.00	51.60	99.96	100.00	0.51	0.00	0.00	1.08	0.00	0.00
100 150	$5.00 \\ 4.94$	3.89	5.00	99.84	77.36	100.00	0.00	0.02	0.00	0.00	0.03	$0.00 \\ 0.01$
	otive LAS	5.00	4.85	98.80	100.00	96.80	0.00	0.00	0.01	0.00	0.00	0.01
50	2.79	5.00	5.00	51.88	99.88	100.00	0.44	0.00	0.00	0.44	0.00	0.00
100	5.00	4.16	5.00	99.96	82.04	100.00	0.00	0.06	0.00	0.00	0.06	0.00
150	5.03	5.00	4.99	99.44	100.00	99.80	0.04	0.00	0.00	0.03	0.00	0.00
	procedure											
50	4.98	5.00	5.00	99.60	100.00	100.00	0.00	0.00	0.00	0.00	0.00	0.00
100		5.00	5.00	•	100.00	100.00	•	0.00	0.00		0.00	0.00
150			5.00			100.00	•		0.00		•	0.00
	ber of Fa											
	ous LAS											
50	2.96	3.98	4.38	54.80	79.60	87.60	0.49	0.00	0.00	0.61	0.00	0.00
100	3.26	4.38	4.54	65.20	87.20	90.80	0.00	0.02	0.00	0.00	0.03	0.00
150	3.52	4.30	4.78	68.80	86.00	95.60	0.06	0.00	0.00	0.07	0.00	0.00
	otive LAS		/	40.04	00.50	00.00	0.00	0.01	0.00	0.49	0.01	0.00
50 100	$\frac{2.44}{4.93}$	$4.93 \\ 3.25$	$5.00 \\ 4.99$	46.24 98.40	98.56 64.64	99.96 99.80	$0.29 \\ 0.01$	$0.01 \\ 0.02$	$0.00 \\ 0.00$	$0.43 \\ 0.01$	$0.01 \\ 0.03$	0.00
150	$\frac{4.93}{4.85}$	4.98	4.18	97.00	99.68	83.28	0.00	0.02	0.00	0.01	0.00	0.00
	otive LAS			31.00	33.00	03.20	0.00	0.00	0.01	0.00	0.00	0.01
50	2.70	5.01	5.00	49.64	100.00	99.96	0.48	0.02	0.00	0.88	0.02	0.00
100	4.94	3.90	5.00	98.84	77.56	99.96	0.00	0.02	0.00	0.00	0.04	0.00
150	4.92	4.98	4.69	98.44	99.64	93.72	0.00	0.00	0.00	0.00	0.00	0.20
Adap	otive LAS		C)									
50	3.00	4.97	5.00	57.36	99.40	100.00	0.28	0.00	0.00	0.37	0.00	0.00
100	4.90	4.71	5.00	97.96	94.20	100.00	0.00	0.00	0.00	0.00	0.00	0.00
150	4.88	4.95	4.97	97.56	99.08	99.40	0.00	0.00	0.00	0.00	0.00	0.00
	procedure		1.00	0= 00	00.04	02.00	0.00	0.00	0.00	0.00	0.00	0.00
50	4.39	4.46	4.63	87.68	$89.24 \\ 82.28$	$92.60 \\ 87.12$	0.02	0.00	0.00	0.02	0.00	0.00
100 150	•	4.13	$4.36 \\ 4.08$	•	. 02.20	81.48	•	0.01	$0.00 \\ 0.00$	•	0.01	$0.00 \\ 0.00$
	ber of Fa	ctors: 5	4.00	•	•	01.40	•	•	0.00	•	•	0.00
	ous LAS		' nobust)									
50	5.04	4.98	5.00	98.40	99.60	100.00	0.27	0.00	0.00	0.27	0.00	0.00
100	4.72	5.00	5.00	94.00	100.00	100.00	0.02	0.00	0.00	0.27	0.00	0.00
150	4.70	4.96	5.00	93.60	99.20	100.00	0.02	0.00	0.00	0.02	0.00	0.00
	otive LAS								0.00			
50	4.97	4.98	4.99	98.80	99.56	99.88	0.07	0.00	0.00	0.07	0.00	0.00
100	3.25	5.03	5.00	64.88	99.24	100.00	0.01	0.08	0.00	0.01	0.07	0.00
150	3.33	3.28	5.09	66.16	65.36	99.96	0.01	0.01	0.06	0.01	0.01	0.06
	ptive LAS											
50	4.99	4.98	4.99	98.96	99.64	99.88	0.09	0.00	0.00	0.09	0.00	0.00
100	3.24	5.05	5.00	64.60	99.24	100.00	0.01	0.09	0.00	0.01	0.09	0.00
150	3.32	3.27	5.09	66.08	65.12	99.96	0.01	0.01	0.06	0.01	0.01	0.06
	otive LAS			00.10	00.64	99.80	0.00	0.00	0.00	0.00	0.00	0.00
$\frac{50}{100}$	$5.00 \\ 3.12$	$4.98 \\ 5.04$	$4.99 \\ 5.00$	99.12 62.36	99.64 99.28	99.80 100.00	$0.09 \\ 0.01$	$0.00 \\ 0.08$	$0.00 \\ 0.00$	$0.09 \\ 0.01$	$0.00 \\ 0.07$	$0.00 \\ 0.00$
150	$\frac{3.12}{3.22}$	$\frac{3.04}{3.18}$	5.00 5.10	64.04	63.44	99.96	0.01	0.08	0.00	0.01	0.07	0.00
	procedure		0.10	01.01	00.11	00.00	0.01	0.01	0.01	0.01	0.01	0.01
50	4.81	4.78	4.83	96.04	95.52	96.36	0.02	0.01	0.03	0.02	0.01	0.03
100		4.78	4.86		95.36	96.56		0.02	0.04		0.02	0.04
150			4.78			94.80	•		0.03			0.03

Table 6: Monte Carlo Results for estimation of Dominant Drivers, Specification 3. The number of dominant Units is 52 ee notes of Table 3 and Table 4.

N/T	50	$\frac{N_d}{100}$	150	50	TPR 100	150	50	FPR 100	150	50	FDR 100	150
	ber of Fa		130	30	100	100	30	100	130	30	100	150
			a breat									
$\frac{\text{rigor}}{50}$	ous Lasse 2.18	4.06	4.58	36.80	81.20	91.60	0.76	0.00	0.00	4.00	0.00	0.00
100	2.16	$\frac{4.00}{2.58}$	2.18	11.20	21.20	38.00	2.21	1.60	0.00	60.57	35.22	6.49
150	5.36	2.94	1.94	3.20	8.80	16.00	3.59	1.72	0.79	91.24	67.20	43.10
	tive Las	so (AIC)										
50	3.56	4.99	5.00	70.40	99.88	100.00	0.10	0.00	0.00	0.10	0.00	0.00
100	5.00	4.27	5.00	99.96	85.32	100.00	0.00	0.00	0.00	0.00	0.00	0.00
150	4.99	5.00	4.84	99.88	100.00	96.68	0.00	0.00	0.00	0.00	0.00	0.00
	otive Lass 3.29	5.00	5.00	65.24	99.92	100.00	0.06	0.00	0.00	0.07	0.00	0.00
50 100	5.29 5.00	$\frac{3.00}{4.55}$	5.00	100.00	99.92	100.00	$0.06 \\ 0.00$	$0.00 \\ 0.01$	0.00	$0.07 \\ 0.00$	$0.00 \\ 0.01$	0.00
150	5.00	5.00	4.96	100.00	100.00	99.28	0.00	0.00	0.00	0.00	0.00	0.00
	otive Lass		1.00	100.00	100.00	00.20	0.00	0.00	0.00	0.00	0.00	
50	4.17	5.00	4.99	82.84	99.96	99.72	0.06	0.00	0.00	0.06	0.00	0.00
100	5.00	5.00	5.00	100.00	100.00	100.00	0.00	0.00	0.00	0.00	0.00	0.00
150	5.00	5.00	5.00	100.00	100.00	100.00	0.00	0.00	0.00	0.00	0.00	0.00
	vnlees and											
50	5.05	5.02	5.03	100.00	100.00	100.00	0.11	0.04	0.06	0.10	0.04	0.06
100		5.04	5.05	•	100.00	100.00	•	0.04	0.05	•	0.04	0.05
150 Num	hor of Ea	otora, 1	5.09	•	•	100.00	•	•	0.06	•	•	0.06
	ber of Fa		1									
	ous Lasso			40.00	70.00	00.00	0.00	0.00	0.00	0.00	0.00	0.00
50 100	$\frac{2.48}{1.68}$	$\frac{3.90}{2.52}$	$\frac{4.04}{2.84}$	49.60	$78.00 \\ 50.40$	80.80	$0.00 \\ 0.00$	$0.00 \\ 0.00$	$0.00 \\ 0.00$	$0.00 \\ 0.00$	$0.00 \\ 0.00$	$0.00 \\ 0.00$
150	1.50	$\frac{2.52}{1.70}$	$\frac{2.84}{2.22}$	33.60 29.60	34.00	56.80 44.40	0.00	0.00	0.00	0.00	0.00	0.00
	otive Las		2.22	29.00	34.00	44.40	0.01	0.00	0.00	0.03	0.00	0.00
50	3.71	4.99	5.00	73.44	99.80	100.00	0.09	0.00	0.00	0.12	0.00	0.00
100	4.92	4.54	5.00	98.24	90.80	99.96	0.00	0.00	0.00	0.00	0.00	0.00
150	4.94	4.97	4.95	98.68	99.40	98.92	0.01	0.00	0.00	0.01	0.00	0.00
Adap	otive Las	so (AICC	C)									
50	3.68	4.99	5.00	72.40	99.80	99.96	0.14	0.00	0.00	0.17	0.00	0.00
100	4.81	4.79	5.00	96.04	95.72	99.96	0.01	0.00	0.00	0.01	0.00	0.00
150	4.85	4.93	4.98	96.60	98.56	99.64	0.01	0.00	0.00	0.01	0.00	0.00
	otive Las		1.00	00.50	00.00	00.00	0.01	0.00	0.00	0.01	0.00	
50	4.33	4.98	4.99	86.52	99.68	99.88	0.01	0.00	0.00	0.01	0.00	0.00
100	4.73	4.83	5.00	94.48	96.48	100.00	0.01	0.01	0.00	0.01	0.01	0.00
150 Prov	4.77	4.84	4.87	95.16	96.40	96.92	0.01	0.01	0.01	0.01	0.01	0.01
50	5.01	4.99	5.01	98.84	99.12	99.20	0.15	0.08	0.11	0.15	0.08	0.11
100	5.01	4.94	4.96		97.40	97.96	0.15	0.03	0.11	0.15	0.03	0.11
150			4.90			96.36			0.05			0.05
	ber of Fa	ctors: 5		· · ·							· · · · · · · · · · · · · · · · · · ·	
	ous Lasse		obust)									
50	2.84	3.70	3.90	54.80	72.00	78.00	0.22	0.22	0.00	0.22	0.22	0.00
100	3.02	3.60	3.98	60.40	72.00	79.20	0.00	0.00	0.02	0.00	0.00	0.02
150	3.02	3.90	4.06	60.00	77.20	81.20	0.01	0.03	0.00	0.01	0.04	0.00
	otive Las											
50	4.68	4.49	4.66	89.48	89.72	93.20	0.47	0.00	0.00	0.45	0.00	0.00
100	3.62	4.71	4.78	70.20	86.52	95.56	0.12	0.41	0.00	0.14	0.40	0.00
150	3.91	3.83	4.42	73.16	73.20	81.20	0.17	0.12	0.25	0.19	0.13	0.25
$\frac{\text{Adap}}{50}$	otive Lass			83.88	90 F0	93.08	0.74	0.00	0.00	0.71	0.00	0.00
50 100	$4.53 \\ 3.59$	$4.48 \\ 4.69$	$\frac{4.65}{4.78}$	83.88 69.68	89.52 84.16	93.08 95.56	$0.74 \\ 0.11$	$0.00 \\ 0.50$	$0.00 \\ 0.00$	$0.71 \\ 0.13$	$0.00 \\ 0.49$	0.00
150	$\frac{3.39}{3.87}$	$\frac{4.09}{3.83}$	4.78	72.60	73.08	95.56 80.56	$0.11 \\ 0.17$	$0.30 \\ 0.12$	$0.00 \\ 0.28$	0.13	0.49 0.14	0.00
	otive Las		1.77	12.00	10.00	00.00	0.11	0.12	0.20	0.10	0.17	0.20
50	4.53	4.34	4.59	83.88	86.80	91.76	0.75	0.00	0.00	0.72	0.00	0.00
100	3.48	4.77	4.71	67.76	81.04	94.28	0.09	0.76	0.00	0.11	0.74	0.00
150	3.75	3.75	4.61	70.80	71.88	74.72	0.14	0.11	0.61	0.16	0.13	0.60
	vnlees and	d Meeste										
50	4.84	4.88	4.86	96.56	97.48	97.08	0.02	0.01	0.01	0.02	0.01	0.01
100		4.87	4.85		96.84	96.56		0.03	0.02		0.02	0.02
150	•	•	4.78	•	•	95.16	•	•	0.01	•	•	0.01
					_	_					_	

Table 7: Monte Carlo Results for estimation of Dominant Drivers, Specification 4. The number of dominant Units is 53%ee notes of Table 3 and Table 4.

N/T	N_d	50	$\frac{\hat{N_d}}{100}$	150	50	TPR 100	150	50	FPR 100	150	50	FDR 100	150
		actors: 0	100	100		100	100		100	100		100	100
		SSO (HAC	C robust)										
50	5	3.28	4.58	4.93	63.80	91.40	98.18	0.20	0.02	0.04	0.21	0.03	0.04
100	10	4.95	7.70	8.22	49.26	77.00	82.20	0.02	0.00	0.00	0.04	0.00	0.00
150 Ada	15	7.48 .SSO (AIC	10.05	11.66	49.80	66.93	77.73	0.01	0.01	0.00	0.01	0.01	0.00
50	5	2.49	4.98	5.00	42.48	99.68	100.00	0.82	0.00	0.00	2.17	0.00	0.00
100	10	9.58	4.06	10.00	95.60	39.18	100.00	0.02	0.16	0.00	0.02	0.23	0.00
150	15	13.36	14.96	6.28	88.33	99.75	41.56	0.08	0.00	0.04	0.08	0.00	0.04
50 Adap	5	SSO (AIC 2.48	5.00	5.00	40.72	100.00	100.00	0.98	0.00	0.00	2.82	0.00	0.00
100	10	9.81	4.01	10.00	97.88	39.10	100.00	0.03	0.11	0.00	0.03	0.21	0.00
150	15	14.32	15.00	6.02	94.61	100.00	39.96	0.09	0.00	0.02	0.15	0.00	0.03
		SSO (BIC			10.10	100.00	100.00	0.00	0.00	0.00	0.15	0.00	0.00
50 100	5 10	$\frac{2.44}{9.70}$	$5.00 \\ 4.31$	5.00 10.00	42.48 96.66	100.00 42.02	100.00 100.00	$0.69 \\ 0.03$	$0.00 \\ 0.12$	$0.00 \\ 0.00$	$\frac{2.17}{0.03}$	$0.00 \\ 0.17$	0.00
150	15	13.80	14.96	9.55	91.64	99.65	63.39	0.03	0.12	0.00	0.05	0.17	0.00
	procedu							0.0.	0.0-	0.00	0.00	0.00	
50	5	4.99	5.00	5.00	99.60	100.00	100.00	0.02	0.00	0.00	0.02	0.00	0.00
100	10	•	10.00	10.00		100.00	100.00 100.00		0.00	0.00		0.00	0.00
150 Num	15 ber of F	actors: 1	•	15.00	•	•	100.00	•		0.00	•	•	0.00
		SSO (HAC	'robuet										
50	ous LAS	2.89	4.13	4.46	56.60	82.20	89.20	0.13	0.04	0.00	0.19	0.04	0.00
100	10	6.61	8.50	9.22	65.90	84.80	92.10	0.02	0.02	0.01	0.02	0.02	0.01
150	15	10.54	13.36	13.55	70.27	88.87	90.27	0.00	0.02	0.01	0.00	0.02	0.01
		SSO (AIC	/	F 00	41.04	00.50	100.00	0.00	0.01	0.00	0.01	0.01	0.00
$\frac{50}{100}$	5 10	2.50 9.77	$\frac{4.94}{7.58}$	5.00 10.00	41.24 97.66	$98.76 \\ 75.32$	100.00 99.98	$0.98 \\ 0.00$	$0.01 \\ 0.05$	$0.00 \\ 0.00$	2.01 0.00	$0.01 \\ 0.05$	$0.00 \\ 0.00$
150	15	14.79	14.88	14.97	98.52	99.13	99.80	0.01	0.01	0.00	0.01	0.01	0.00
Adap		SSO (AIC	CC)										
50	5	2.60	5.00	5.00	41.08	99.92	100.00	1.20	0.00	0.00	2.73	0.00	0.00
100 150	10 15	$9.76 \\ 14.74$	$9.54 \\ 14.87$	10.00 14.96	97.34 98.13	95.26 99.07	100.00 99.72	$0.03 \\ 0.02$	$0.01 \\ 0.01$	$0.00 \\ 0.00$	$0.03 \\ 0.02$	$0.01 \\ 0.01$	$0.00 \\ 0.00$
		SSO (BIC		14.50	30.13	33.01	33.12	0.02	0.01	0.00	0.02	0.01	0.00
50	5	2.88	4.98	5.00	49.92	99.68	100.00	0.84	0.00	0.00	1.30	0.00	0.00
100	10	9.72	9.89	10.00	96.88	98.80	100.00	0.03	0.01	0.00	0.03	0.01	0.00
150 DM	15	14.71	14.83	14.94	97.97	98.76	99.59	0.01	0.01	0.00	0.01	0.01	0.00
$\frac{BM}{50}$	procedu 5	4.46	4.77	4.75	88.92	95.16	94.84	0.04	0.02	0.02	0.03	0.02	0.02
100	10		9.99	10.00		99.92	99.96	0.04	0.00	0.00		0.02	0.00
150	15			15.00			99.99			0.00			0.00
		actors: 5											
		SSO (HAC			07.00	00.10	100.00	0.05	0.00	0.00	0.05	0.00	0.00
50 100	5 10	4.88 10.00	4.97	5.00 10.00	97.00 99.90	99.40	100.00 100.00	0.07	0.00	0.00	$0.07 \\ 0.01$	0.00	0.00
150	10 15	15.00 15.00	10.01 15.00	10.00 14.98	100.00	$100.00 \\ 35.07$	33.99	$0.01 \\ 0.00$	$0.01 \\ 6.06$	$0.00 \\ 5.84$	0.01	$0.01 \\ 38.78$	33.93
		SSO (AIC				55.01	55.00	2.00		2.01	2.00		
50	5	5.09	5.00	5.00	99.96	99.88	100.00	0.20	0.01	0.00	0.20	0.01	0.00
100	10	6.64	9.56	10.00	66.36	95.62	100.00	0.00	0.00	0.00	0.00	0.00	0.00
150	15	8.64 .SSO (AIC	9.05	14.70	57.61	60.31	98.01	0.00	0.00	0.00	0.00	0.00	0.00
50	5	5.10	5.00	5.00	100.00	99.88	100.00	0.21	0.01	0.00	0.21	0.01	0.00
100	10	6.56	9.58	10.00	65.58	95.78	100.00	0.00	0.00	0.00	0.00	0.00	0.00
150	15	8.44	9.03	14.70	56.29	60.21	98.03	0.00	0.00	0.00	0.00	0.00	0.00
		SSO (BIC	/	F 00	100.00	99.80	100.00	0.14	0.01	0.00	0.14	0.01	0.00
$\frac{50}{100}$	5 10	5.06 6.43	$4.99 \\ 9.56$	5.00 10.00	$100.00 \\ 64.28$	99.80 95.58	100.00 100.00	$0.14 \\ 0.00$	$0.01 \\ 0.00$	$0.00 \\ 0.00$	$0.14 \\ 0.00$	$0.01 \\ 0.00$	$0.00 \\ 0.00$
150	15	8.27	8.67	14.51	55.16	57.79	96.76	0.00	0.00	0.00	0.00	0.00	0.00
	procedu												
50	5	4.81	4.84	4.83	95.92	96.60	96.24	0.02	0.02	0.04	0.02	0.02	0.04
100 150	10 15		9.58	$9.25 \\ 13.93$		95.78	92.54 92.89		0.00	$0.00 \\ 0.00$		0.00	$0.00 \\ 0.00$
100	10	•	•	10.30	•	•	∂4.0∂	•		0.00	•	•	0.00

Table 8: Monte Carlo Results for estimation of Dominant Units: Number of dominant Units is $\lceil 0.1N \rceil$, Specification 5. See notes of Table 3 and Table 4.

			- Î			mp.p.			EDD			EDD	
N/T	N_d	50	$\frac{\hat{N_d}}{100}$	150	50	TPR 100	150	50	FPR 100	150	50	FDR 100	150
		factors: 0											
		SSO (HAC	robust)										
50	25	7.26	10.73	14.35	28.52	42.48	57.28	0.52	0.44	0.12	0.71	0.61	0.16
100	50 75	$16.92 \\ 26.88$	24.63 36.89	28.60	$33.72 \\ 35.84$	49.22	57.18	0.12	0.04	$0.02 \\ 0.01$	0.18	0.06	$0.03 \\ 0.02$
$\frac{150}{\text{Adar}}$		$\frac{20.88}{\text{ASSO (AIC}}$		39.14	33.84	49.17	52.17	0.00	0.01	0.01	0.00	0.02	0.02
50	25	6.47	24.82	24.96	25.68	99.28	99.82	0.22	0.00	0.00	0.35	0.00	0.00
100	50	40.11	10.39	49.97	80.21	20.73	99.94	0.00	0.04	0.00	0.00	0.06	0.00
150	75	60.00 SSO (AIC	73.29	19.76	80.01	97.72	26.33	0.00	0.00	0.01	0.00	0.00	0.01
50	25	7.25	24.89	24.96	28.50	99.57	99.86	0.50	0.00	0.00	0.81	0.00	0.00
100	50	12.29	15.93	50.00	24.53	31.77	100.00	0.04	0.10	0.00	0.05	0.16	0.00
150	75	6.95	32.29	54.46	9.23	43.05	72.61	0.04	0.00	0.00	0.05	0.00	0.00
Adap 50	otive LA 25	SSO (BIC 6.63		24.96	26.31	99.39	99.83	0.21	0.00	0.00	0.33	0.00	0.00
100	50	21.30	24.85 13.56	49.99	$\frac{20.31}{42.59}$	99.39 27.06	99.83	0.21 0.01	0.00	0.00	0.33 0.01	0.00	0.00
150	75	33.50	13.64	36.51	44.67	18.19	48.69	0.00	0.00	0.00	0.00	0.00	0.00
BM j	procedu	re											
50	25	23.12	24.93	24.98	92.49	99.71	99.93	0.00	0.00	0.00	0.00	0.00	0.00
$\frac{100}{150}$	50 75	•	49.86	$50.00 \\ 75.00$		99.71	100.00 100.00		0.00	$0.00 \\ 0.00$	•	0.00	$0.00 \\ 0.00$
		actors: 1	•	10.00	•	•	100.00	*	*	0.00	•	•	0.00
		SSO (HAC	robust)										
50	25	8.64	12.85	16.98	34.32	51.36	67.92	0.24	0.04	0.00	0.34	0.05	0.00
100	50	16.05	23.35	29.23	32.08	46.70	58.46	0.02	0.00	0.00	0.03	0.00	0.00
150	75	19.07 SSO (AIC	28.28	33.41	25.43	37.71	44.55	0.00	0.00	0.00	0.00	0.00	0.00
50	25	17.64	24.28	24.55	70.51	97.12	98.20	0.05	0.00	0.00	0.05	0.00	0.00
100	50	28.05	49.79	49.89	56.10	99.58	99.78	0.00	0.00	0.00	0.00	0.00	0.00
150	75	17.73	37.87	74.68	23.64	50.49	99.57	0.00	0.00	0.00	0.00	0.00	0.00
		ASSO (AIC		04.55	01.00	07.10	00.00	0.00	0.00	0.00	0.00	0.00	0.00
50 100	25 50	20.26 15.78	24.30 46.82	24.57 49.99	81.02 31.56	97.18 93.63	98.28 99.98	0.00 0.00	0.00	0.00	0.00	$0.00 \\ 0.00$	0.00
150	75	15.78	30.30	71.64	21.04	40.41	95.52	0.00	0.00	0.00	0.00	0.00	0.00
	otive LA	SSO (BIC											
50	25	20.67	24.12	24.38	82.67	96.48	97.52	0.02	0.00	0.00	0.02	0.00	0.00
$\frac{100}{150}$	50 75	23.95 19.07	$48.77 \\ 34.23$	49.99 71.14	$47.90 \\ 25.42$	97.54 45.64	99.98 94.85	$0.00 \\ 0.00$	$0.00 \\ 0.00$	$0.00 \\ 0.00$	$0.00 \\ 0.00$	$0.00 \\ 0.00$	$0.00 \\ 0.00$
	procedu		34.23	11.14	20.42	45.04	94.60	0.00	0.00	0.00	0.00	0.00	0.00
50	25	8.84	10.15	11.39	35.36	40.58	45.56	0.00	0.00	0.00	0.00	0.00	0.00
100	50	•	13.81	16.52		27.62	33.04	•	0.00	0.00	•	0.00	0.00
150	75		•	19.53			26.04	•		0.00	•	•	0.00
		actors: 5	Y 1										
$\frac{\text{rigor}}{50}$	ous LAS	SSO (HAC 24.94	25.00	25.00	69.98	67.87	66.95	41.21	41.17	41.13	96.90	83.80	78.89
100	50	24.94	50.00	50.00	34.19	69.17	69.99	21.55	40.73	40.05	59.90	84.81	80.92
150	75	22.46	74.98	75.00	16.97	64.89	67.07	13.87	43.05	41.64	25.06	93.04	85.45
		ASSO (AIC		20.50		70.00	00.00	0.00	0.00	0.00	0.00	0.00	0.00
50 100	25 50	13.94 11.81	18.41 22.00	20.72 23.69	55.77 23.62	73.63 44.00	82.89 47.37	0.00 0.00	0.00	0.00	0.00 0.00	0.00	0.00
150	75	13.41	14.61	28.11	$\frac{25.02}{17.88}$	19.48	37.49	0.00	0.00	0.00	0.00	0.00	0.00
		SSO (AIC											
50	25	12.84	17.87	20.53	51.38	71.50	82.10	0.00	0.00	0.00	0.00	0.00	0.00
100	50 75	$11.32 \\ 12.64$	22.05	22.93	22.63	44.11	45.87	0.00	0.00	0.00	0.00	0.00	0.00
150 Adar	75 otive LA	SSO (BIC	14.58	27.78	16.85	19.44	37.04	0.00	0.00	0.00	0.00	0.00	0.00
50	25	13.05	16.22	19.20	52.19	64.87	76.80	0.00	0.00	0.00	0.00	0.00	0.00
100	50	11.25	21.12	19.69	22.51	42.24	39.39	0.00	0.00	0.00	0.00	0.00	0.00
150	75	12.83	14.28	27.72	17.10	19.05	36.96	0.00	0.00	0.00	0.00	0.00	0.00
$\frac{\text{BM }_{1}}{50}$	procedu 25	3.64	3.58	3.74	14.55	14.34	14.97	0.00	0.00	0.00	0.00	0.00	0.00
100	25 50	3.04	$\frac{3.58}{2.64}$	$\frac{3.74}{3.07}$	14.55	$\frac{14.34}{5.28}$	6.13	0.00	0.00	0.00	0.00	0.00	0.00
150	75			2.83			3.78			0.00	•		0.00

Table 9: Monte Carlo Results for estimation of Dominant Units: Number of dominant Units is $\lceil 0.5N \rceil$, Specification 52.5. See notes of Table 3 and Table 4.

No. No.							mp.p.							
Number of Factors 0	N/T	Ν,	50		150	50		150	50		150	50		150
Figorous LASSO (HAC robust)				100	100		100	100		100	100		100	100
The color of the				robust)										
150 135 8.50 8.78 14.50 6.29 6.50 10.74 0.07 0.00 0.00 0.01 0.00					7.66	13.53	16.16	16.33	5.20	8.40	6.20	5.38	8.11	5.26
Adaptive LASSO (AIC)						9.91								
Section Column					14.50	6.29	6.50	10.74	0.07	0.00	0.00	0.14	0.00	0.00
100 90 3.72 3.94 4.49 4.13 4.88 4.99 0.00 0.0			,		6.07	11.38	11.40	13.48	0.08	0.00	0.00	0.12	0.00	0.00
Adaptive LASSO (AICC)														
Section Sect					3.08	2.96	2.45	2.28	0.00	0.00	0.00	0.00	0.00	0.00
100					C 02	11.05	11.00	19.04	0.20	0.00	0.00	0.40	0.00	0.00
150														
Section Sect														
100 90 3.84 4.39 4.08 4.27 4.88 4.54 0.00 0.0														
135 3.75 4.75 2.99 2.78 3.51 2.21 0.00 0														
BM procedure														
Section Sect				1.10	2.00	2.10	0.01	2.21	0.00	0.00	0.00	0.00	0.10	0.00
Number of Factors:	50	45	3.29			7.32			0.00			0.00		
Number of Factors: 1 Figorous LASSO (HAC robust) Figorous LA						•								
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $				•	2.74	•	•	2.03	•	•	0.00	•	·	0.00
The color of the				robust)										
150					5.29	12.16	15.33	11.73	0.60	0.20	0.20	0.85	0.27	0.28
Adaptive LASSO (AIC)	100	90			3.96	6.71	6.04	4.40	0.00	0.00	0.00	0.00	0.00	0.00
The color of the					4.22	3.37	2.39	3.13	0.00	0.00	0.00	0.00	0.00	0.00
100		tive LA			6.25	0.45	12.28	13.88	0.00	0.00	0.00	0.00	0.00	0.00
150														
The color of the	150	135	5.27	4.46										
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $														
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$														
Adaptive LASSO (BIC) 50														
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	Adap	tive LA	SSO (BIC	!)										
Second Part														
BM procedure														
Society Soci				0.41	4.90	4.00	0.26	3.06	0.00	0.00	0.00	0.00	0.00	0.00
Number of Factors: 5 Number of Factors: 5				8.11	9.69	11.36	18.01	21.52	0.00	0.00	0.00	0.00	0.00	0.00
Number of Factors: 5			•	9.52			10.58			0.00			0.00	
rigorous LASSO (HAC robust) 50 45 34.42 43.20 44.98 74.51 92.76 95.81 67.07 83.81 87.41 216.96 207.49 201.28 100 90 19.36 86.44 88.18 20.96 92.65 94.87 19.01 84.80 86.13 89.32 322.03 281.95 Adaptive LASSO (AIC) Time LASSO (AIC) 50 45 7.88 5.64 5.85 17.50 12.54 13.00 0.				•	11.23	•	•	8.32	•	•	0.00	•	•	0.00
So				nobust)										
100 90 19.36 86.44 88.18 20.96 92.65 94.87 19.01 84.80 86.13 89.32 322.03 281.95 135					44.98	74.51	92.76	95.81	67.07	83.81	87.41	216.96	207.49	201.28
150 135 4.70 39.76 126.94 3.72 28.15 90.03 3.02 26.15 83.30 16.86 119.87 340.04		90	19.36	86.44		20.96							322.03	
50 45 7.88 5.64 5.85 17.50 12.54 13.00 0.00					126.94	3.72	28.15	90.03	3.02	26.15	83.30	16.86	119.87	340.04
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$					F 0F	17.50	10.54	12.00	0.00	0.00	0.00	0.00	0.00	0.00
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$														
Adaptive LASSO (AICC) 50 45 11.67 5.92 6.42 25.92 13.16 14.27 0.00														
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$														
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$														
Adaptive LASSO (BIC) 50 45 11.40 5.99 5.65 25.32 13.31 12.56 0.00														
50 45 11.40 5.99 5.65 25.32 13.31 12.56 0.00 <td< td=""><td></td><td></td><td></td><td></td><td>20.00</td><td>10.70</td><td>12.10</td><td>10.00</td><td>0.00</td><td>0.00</td><td>0.00</td><td>0.00</td><td>0.00</td><td>0.00</td></td<>					20.00	10.70	12.10	10.00	0.00	0.00	0.00	0.00	0.00	0.00
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	50	45	11.40	5.99										
BM procedure 50 45 2.58 2.67 2.61 5.72 5.94 5.79 0.00														
50 45 2.58 2.67 2.61 5.72 5.94 5.79 0.00 0.00 0.00 0.00 0.00 0.00 0.00 100 90 . 2.19 2.32 . 2.43 2.58 . 0.00 0.00 . 0.00 0.00				16.58	26.51	10.74	12.28	19.64	0.00	0.00	0.00	0.00	0.00	0.00
100 90 . 2.19 2.32 . 2.43 2.58 . 0.00 0.00 . 0.00 0.00				2.67	2.61	5.72	5.94	5.79	0.00	0.00	0.00	0.00	0.00	0.00
<u>150</u> 135 2.17 1.61 0.00 0.00	100	90			2.32			2.58			0.00			0.00
	150	135		•	2.17			1.61			0.00			0.00

Table 10: Monte Carlo Results for estimation of Dominant Units: Number of dominant Units is $\lceil 0.9N \rceil$, Specification 55. See notes of Table 3 and Table 4.

C Empirical Application

Abbreviation	Countryname		
arg	Argentina	mex	mexico
austlia	Australia	neth	Netherlands
austria	Austria	nor	Norway
bel	Belgium	nzld	New zealand
bra	Brazil	per	Peru
can	Canada	phlp	Philippines
china	China	safrc	South Africa
chl	Chile	sarbia	Saudi Arabia
fin	Finland	sing	Singapore
france	France	spain	Spain
germ	Germany	swe	Sweden
india	India	switz	Switzerland
indns	Indonesia	thai	Thailand
italy	Italy	turk	Turkey
japan	Japan	uk	United Kingdom
kor	Korea	usa	United States
mal	Malaysia		

Table 11: Countries in the GVAR dataset.

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CAMP Working Paper Series ISSN: 1892-2198

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