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# Nowcasting GDP in Real-Time: A Density Combination Approach \*

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## Abstract

In this paper we use U.S. real-time vintage data and produce combined density nowcasts for quarterly GDP growth from a system of three commonly used model classes. The density nowcasts are combined in two steps. First, a wide selection of individual models within each model class are combined separately. Then, the nowcasts from the three model classes are combined into a single predictive density. We update the density nowcast for every new data release throughout the quarter, and highlight the importance of new information for the evaluation period 1990Q2-2010Q3. Our results show that the logarithmic score of the predictive densities for U.S. GDP increase almost monotonically as new information arrives during the quarter. While the best performing model class is changing during the quarter, the density nowcasts from our combination framework is always performing well both in terms of logarithmic scores and calibration tests. The density combination approach is superior to a simple model selection strategy and also performs better in terms of point forecast evaluation than standard point forecast combinations.

**JEL-codes:** C32, C52, C53, E37, E52.

**Keywords:** Density combination; Forecast densities; Forecast evaluation; Monetary policy; Nowcasting; Real-time data

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# 1 Introduction

Policy decisions in real-time are based on assessments of the recent past and current economic condition under a high degree of uncertainty. Many key statistics are released with a long delay, are subsequently revised and are available at different frequencies. In addition, the data generating process is unknown and is likely to change over time. As a consequence, there has been a substantial interest in developing a framework for forecasting the present and recent past, i.e. nowcasting.<sup>1</sup>

Until now, the academic literature on nowcasting has been focusing on developing single models that increase forecast accuracy in terms of point nowcast, see among others [Evans \(2005\)](#) and [Giannone et al. \(2008\)](#). This differs in two important ways from policy making in practice. First, policy makers are often provided with several different models which may provide rather different forecasts. This leads naturally to the question of model choice or combination.<sup>2</sup> Second, if the policy maker's loss function is not quadratic or if the world is nonlinear then it no longer suffices to focus solely on first moments of possible outcomes (point forecasts). To ensure appropriate monetary policy decisions, central banks therefore must provide suitable characterizations of forecast uncertainty. Density forecasts provide an estimate of the probability distribution of the forecasts.<sup>3</sup>

In this paper we use a density combination framework to produce density nowcasts for U.S. GDP from a system of three different model classes. To ensure relevance for policy makers, we include vector autoregressive models (VARs), leading indicator models and factor models. These three model classes are the most widely used for short-term forecasting at central banks. Our recursive nowcasting exercise is applied to U.S. real-time vintage data. We update the density nowcasts for every new data release during a quarter and highlight the importance of new data releases for the evaluation period 1990Q2-2010Q3.

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<sup>1</sup>See [Banbura et al. \(2011\)](#) for a survey on nowcasting.

<sup>2</sup>The idea of combining forecasts from different models was first introduced by [Bates and Granger \(1969\)](#). Their main conclusion is that a combination of two forecasts can yield lower mean square forecasts error than either of the original forecasts when optimal weights are used. [Timmermann \(2006\)](#) surveys combination methods and provides theoretical rationales in favor of combination - including unknown instabilities, portfolio diversification of models and idiosyncratic biases.

<sup>3</sup>[Mitchell and Hall \(2005\)](#) and [Hall and Mitchell \(2007\)](#) provide some justification for density combination, while [Gneiting \(2011\)](#) discusses the difference between point forecasting and density forecasting.

The density nowcasts are combined in a two-step procedure. In the first step, we group models into different model classes. The nowcasts from all individual models within a model class are combined using the logarithmic score (log score) to compute the weights, see among others [Jore et al. \(2010\)](#). This yields a combined predictive density nowcast for each of the three model classes. In a second step, these three predictive densities are combined into a single density nowcast, again using log score weights. The advantage of this approach is that it explicitly accounts for uncertainty about model specification and instabilities within each model class, as well as a priori giving equal weight to each model class. We evaluate our density nowcasts both in terms of scoring rules and the probability integral transform to check whether the predictive densities are accurate and well-calibrated.

Our results extends the findings in the earlier nowcasting and model combination literature along several dimensions:

First, we show that the log score of the predictive densities for the model combination and all three model classes increases almost monotonically as new information arrives during the quarter, while the densities seem well-calibrated at each point in time. [Evans \(2005\)](#), [Giannone et al. \(2008\)](#) and [Aruoba et al. \(2009\)](#) evaluate point forecasts from individual models and highlight the importance of using non-synchronous data releases (jagged edge problem) for nowcasting. Our analysis confirms these results by evaluating density forecasts in a model combination framework. Our results also supplement the findings in e.g. [Bache et al. \(2011\)](#), [Amisano and Geweke \(2009\)](#) and [Gerdrup et al. \(2009\)](#), who all study density combination methods, but not nowcasting.

Second, while the ranking of the model classes is changing during the quarter and in accordance with new data releases, the model combination is always performing well. In particular, our density combination framework performs much better than a simple selection strategy. This result extends on the results reported in e.g. [Rünstler et al. \(2009\)](#) who study point forecasts and model selection strategies.

Third, the density combination framework also performs better in terms of point forecast evaluation than standard point forecast combination methods.<sup>4</sup> As new information arrives throughout the quarter, the log score weights adapt faster than standard point forecast weights

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<sup>4</sup>See e.g. [Faust and Wright \(2009\)](#) for a recent real-time application of a point forecast combination framework.

(e.g. MSE weights and equal weights). In this way, our combination procedure attaches a higher weight to models with new and relevant information. This finding motivates the potential leverage of density evaluation over simple point forecast evaluation when the goal is to maximize forecast accuracy in a nowcasting framework. The paper most closely related to ours is [Mitchell et al. \(2010\)](#). They combine a small set of leading indicator models to forecast the 2008-2009 Euro area recession.

Our results are robust to a number of robustness checks. Computing the model weights and evaluating the final densities using different real-time data vintages do not alter the qualitative results. The performance of our density combination framework is actually more robust to real-time data issues than any of the individual models. Further, changing the weighting scheme using a one step procedure and/or equal weights have no effect on our conclusions: The performance almost monotonically increase throughout the quarter as new information becomes available, and the combination approach is still superior to the selection strategy.

The rest of the paper is organized as follows. In the next section we describe the real-time data set. In the third section we describe the modeling framework and discuss the rationale for combining densities for different model classes, while the fourth section describes the recursive forecasting exercise. The fifth section contains the results of the out-of-sample nowcasting experiment. Finally, we conclude in the sixth section.

## 2 Data

Our aim is to evaluate the current quarter density nowcast of the quarterly growth rate of GDP, on the basis of the flow of information that becomes available during the quarter. Within each quarter, the contemporaneous value of GDP growth can be forecasted using higher frequency variables that are published in a more timely manner than GDP itself. The large monthly and quarterly data set relevant for a given nowcast changes throughout the quarter.

The monthly raw data are mainly collected from the ALFRED (Archival Federal Reserve Economic Data) database maintained by the Federal Reserve Bank of St. Louis. This database consists of collections of vintages of data for each variable. These vintages vary across time as either new data are released or existing data are revised by the relevant sta-

tistical agency. Using data from this database ensures that we are using only data that were available on the date of the forecast origin. In addition some few real-time data series are collected from the Federal Reserve Bank of Philadelphia’s Real-Time Data Set for Macroeconomists. Only quarterly vintagers are available for these series, where each vintage reflects the information available around the middle of the respective quarter. [Croushore and Stark \(2001\)](#) provide a description of the database.

Some of the series we use are not revised, such as for instance financial market data. Other variables, such as consumer prices and most survey data, only undergo revisions due to changes in seasonal factors. When real-time vintage data are not available for these variables, we use the last available data vintage as their real-time observations. All these data series are collected from Reuters EcoWin. Series such as equity prices, dividend yields, currency rates, interest rates and commodity prices are constructed as monthly averages of daily observations. Finally, for some series such as disaggregated measures of industrial production, there only exist real-time vintage data for parts of the evaluation period. For such variables, we use the first available real-time vintage and truncate these series recursively backwards. A more detailed description of all the data series and the availability of real-time vintages are given in the appendix, section [7.4](#).

The full forecast evaluation period runs from 1990Q2 to 2010Q3. We use monthly real-time data with quarterly vintages from 1990Q3 to 2010Q4.<sup>5</sup> At each forecast origin  $t$ , we use vintage  $t$  data to estimate models and then construct nowcasts for period  $t$ . The starting point of the estimation period is set to 1982M1. We follow [Romer and Romer \(2000\)](#) and use the second available estimate of GDP as actual when evaluating forecast accuracy.<sup>6</sup> The nowcasting exercise is described in more detail in section [4](#).

### 3 Forecast framework

In practice, policymakers are often provided with forecasts from different models. For short-term forecasting, there are in particular three classes of models that are widely used; Vector

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<sup>5</sup>We abstract from data revisions in the monthly variables within a quarter. The quarterly vintages reflects the vintage available just before the first release of GDP.

<sup>6</sup>Our results are robust to alternative definitions of actuals (benchmark GDP vintage). See section [5.3.3](#) for more details.

Autoregressive (VAR) models, leading indicator models (LIM) and factor models (FM).<sup>7</sup> The forecast of interest in this paper are combinations of density nowcasts for quarterly U.S. GDP growth, on the basis of the flow of information that becomes available during the quarter. To ensure relevance to policymakers, we include the three model classes mentioned above in our combination framework.

However, there is considerable uncertainty regarding specifications, such as choosing lag lengths, data-sample, variables to include etc. for each model class. For example, recent work by [Clark and McCracken \(2009\)](#) and [Clark and McCracken \(2010\)](#) show that VARs may be prone to instabilities, and they suggest combining forecasts from a wide set of VARs to circumvent these problems. The same arguments may also apply to factor models and leading indicator models.<sup>8</sup> In this application, we thus include a wide selection of different specifications for each of the three model classes.

As seen in [table 1](#) we include a total of 516 individual models, distributed unevenly into the three model classes. The table also gives a short overview of the different specifications within each model class. In the [appendix 7.2](#) we give a more detailed description of each of the model classes and their specifications.

To utilize the gains from forecast combination without being influenced by the number of models within each class we combine the forecasts in two steps.<sup>9</sup> In the first step, we group models into different model classes. Density nowcasts for each individual model within a model class are then combined. This yields one, combined predictive density for each model class. In the second step, we combine the density nowcasts from each model class and obtain a single combined density nowcast.<sup>10</sup> An advantage of this approach, is that it explicitly accounts for uncertainty about model specification and instabilities within each model class.

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<sup>7</sup>[Bjørnland et al. \(2009\)](#) give a short overview of the forecasting/combination schemes commonly used in central banks.

<sup>8</sup>In particular the number of factors and the choice of a stable leading indicator over a long time horizon are issues of concern.

<sup>9</sup>The forecasting methodology used in this paper resembles the system used at Norges Bank, and commonly referred to as SAM (System for Averaging Models), see [Gerdrup et al. \(2009\)](#) for details. [Garratt et al. \(2009\)](#) also propose to combine the nowcast from a large number of models in a two-step procedure.

<sup>10</sup>Our approach is close to [Aiolfi and Timmermann \(2006\)](#) in the sense that we combine models in more than one stage. They find that forecasting performance can be improved by first sorting models into clusters based on their past performance, second by pooling forecasts within each cluster, and third by estimating optimal weights on these clusters (followed by shrinkage towards equal weights).

Table 1. A summary of all models and model classes

Model class	Description	Number of models
VAR	ARs and VARs using GDP (and inflation and/or interest rate) Lag length: 1 – 4 Transformations: First differences, double differences, detrended Estimation period: Recursive and rolling samples of 20 and 30 observations Combination method: Linear opinion pool and log score weights	144
LIM	Bivariate VARs with GDP and 120 different monthly indicators Lag-length: 1 Transformations: First differences Estimation Period: Recursive and rolling samples of 20 and 30 observations Combination method: Linear opinion pool and log score weights	360
FM	Dynamic Factor Models Number of factors: 1 – 4 Estimation period: Recursive and rolling samples of 20 and 30 observations Combination method: Linear opinion pool and log score weights	12
Combination	Combination method: Linear opinion pool and log score weights	516

*Note: Each of the model classes are described in more detail in the appendix section 7.2. The estimation period starts in 1982M1 for all models.*

Hence, our predictive densities for each model class will be more robust to mis-specification and instabilities than following a common approach where only one model from each model class is used. Further, the two-step procedure ensures that we put a priori equal weight on each model class.

### 3.1 Combining predictive densities

There are two elementary choices when combining predictive densities. The first is what method of aggregation to use, i.e. the functional form of combining. The second is how to construct the weights attached to each model. In the following, we will explain how the predictive densities are combined. In our two-stage approach, we choose the same method of aggregation and construction of weights for both stages (as seen in table 1).



### 3.1.1 Method of aggregation

One popular approach to solve the aggregation problem is to take a linear combination of the individual density forecasts, the so called linear opinion pool:

$$p(y_{\tau,h}) = \sum_{i=1}^N w_{i,\tau,h} g(y_{\tau,h}|I_{i,\tau}), \quad \tau = \underline{\tau}, \dots, \bar{\tau} \quad (1)$$

where  $N$  denotes the number of models to combine,  $I_{i,\tau}$  is the information set used by model  $i$  to produce the density forecast  $g(y_{\tau,h}|I_{i,\tau})$  for variable  $y$  at forecasting horizon  $h$ .  $\underline{\tau}$  and  $\bar{\tau}$  are the period over which the individual forecasters' densities are evaluated, and finally  $w_{i,\tau,h}$  are a set of non-negative weights that sum to unity (see section 3.1.2).

Combining the  $N$  density forecasts according to equation 1 can potentially produce a combined density forecast with characteristics quite different from those of the individual forecasters. As [Hall and Mitchell \(2007\)](#) notes; if all the individual forecasters' densities are normal, but with different mean and variance, the combined density forecast using the linear opinion pool will be mixture normal. This distribution can accommodate both skewness and kurtosis and be multimodal, see [Kascha and Ravazzolo \(2010\)](#).<sup>11</sup> If the true unknown density is non-normal, this is a appealing feature.

### 3.1.2 Deriving the weights

Many different weighting schemes have been proposed in the literature. Equally-weighted combinations have been found to be surprisingly effective for point forecasting, see [Clemen \(1989\)](#) and [Stock and Watson \(2004\)](#). [Bates and Granger \(1969\)](#) propose another alternative, combining models using weights derived from their sum of squared errors (SSE). These weights will minimise a quadratic loss function based on forecast errors, provided that the estimation errors of different models are uncorrelated. Using inverse-SSE weights produces the same weights as those derived from the inverse of mean squared errors (MSEs) computed over some recent observed sample:

$$w_{i,\tau,h} = \frac{\frac{1}{MSE_{i,\tau,h}}}{\sum_{i=1}^N \frac{1}{MSE_{i,\tau,h}}}, \quad \tau = \underline{\tau}, \dots, \bar{\tau} \quad (2)$$

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<sup>11</sup>Further, since the combined density is a linear combination of all the individual forecasters' densities, the variance of the combined density forecast will in general, and more realistic, be higher than that of individual models. The reason is that the variance of the combination is equal to the weighted sum of a measure of model uncertainty and dispersion (or disagreement) of the point forecast, see [Wallis \(2005\)](#).

where  $\tau, h, N$  and  $i$  are defined above.

In a density combination setting, the range of possible weighting schemes is richer. It is possible to calculate MSEs based on the means of the distributions, but it is more natural to take advantage of the full distributions, see e.g. [Jore et al. \(2010\)](#) and [Amisano and Geweke \(2009\)](#). Then the question of evaluating densities arises.

A popular statistical measure is the Kullback-Leibler divergence or Kullback-Leibler information criterion (KLIC), see [Mitchell and Hall \(2005\)](#), [Amisano and Giacomini \(2007\)](#) and [Kascha and Ravazzolo \(2010\)](#). The KLIC is a sensible measure of accuracy since it chooses the model which on average gives higher probability to events that have actually occurred. As argued by [Mitchell and Hall \(2005\)](#) the KLIC provides a unified framework for evaluating, comparing and combining density forecasts, and [Mitchell and Wallis \(2010\)](#) show that the KLIC can be interpreted as a mean error, similar to the use of the mean error or bias in point forecast evaluation.<sup>12</sup> Specifically, the KLIC distance between the true density  $f$  of a random variable  $y_t$  and some candidate density  $f_i(y_t)$  obtained from the individual model  $i$  is defined as

$$KLIC_i = \int f_t(y_t) \ln \frac{f(y_t)}{f_i(y_t)} dy_t = E[\ln f(y_t) - \ln f_i(y_t)], \quad (3)$$

where  $E$  denotes the expectation. The KLIC difference between two densities is then defined as

$$\begin{aligned} KLIC_i - KLIC_j &= E[\ln f(y_t) - \ln f_i(y_t)] - E[\ln f(y_t) - \ln f_j(y_t)] \\ &= E[\ln f_j(y_t)] - E[\ln f_i(y_t)] \\ &= E \ln S_j - E \ln S_i, \end{aligned} \quad (4)$$

i.e. the difference between two expected log scores. Thus, when  $E \ln S_j > E \ln S_i$ , then  $KLIC_j < KLIC_i$ . Under some regularity conditions,  $E \ln S_i$  can be estimated by the average log score

$$\ln S_i = \frac{1}{T} \sum_{t=1}^T \ln f_i(y_t). \quad (5)$$

It follows from equation 4 that we do not need to know the true density in order to compare two candidate densities. When comparing density forecasts, a measure of out-of-

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<sup>12</sup>As discussed in [Hoeting et al. \(1999\)](#), the log score is a combined measure of bias and calibration.

sample performance is the (out-of-sample) log score given by

$$\ln S_{i,h} = \frac{1}{T-h-T^S+1} \sum_{t=T^S}^{T-h} \ln f_{t+h,t,i}(y_{t+h}), \quad (6)$$

where  $f_{t+h,t,i}$  denotes a prediction of the density for  $Y_{t+h}$  conditional on some information set available at time  $t$ , and  $T^S$  and  $T$  denotes respectively the starting period for the forecasts and number of observations.

Hence, the log score is the logarithm of the probability density function evaluated at the outturn of the forecast. Following [Jore et al. \(2010\)](#) we define the recursive log score weights as:

$$w_{i,\tau,h} = \frac{\exp[\sum_{\underline{\tau}}^{\tau-h} \ln f(y_{\tau,h}|I_{i,\tau})]}{\sum_{i=1}^N \exp[\sum_{\underline{\tau}}^{\tau-h} \ln f(y_{\tau,h}|I_{i,\tau})]} = \frac{\ln S_{i,\tau,h}}{\sum_{i=1}^N \ln S_{i,\tau,h}}, \quad \tau = \underline{\tau}, \dots, \bar{\tau} \quad (7)$$

where  $\tau, h, y, N, i$  and  $g(y_{\tau,h}|I_{i,\tau})$  are defined above. Two points are worth emphasizing about this expression. The weights are derived based on out-of-sample performance, and the weights are horizon specific.

### 3.2 Evaluating density forecasts

[Corradi and Swanson \(2006\)](#) provide an extensive survey of the theoretical literature on density evaluation. In general, the literature is divided in two branches. One branch is concerned with scoring rules and distance measures, where scoring rules evaluate the quality of probability forecasts by assigning a numerical score based on the forecast and the subsequent realization of the variable, see section [3.1.2](#).

Another common approach for evaluating density forecasts provides statistics suitable for test of forecast accuracy relative to the “true” unobserved density. Following [Rosenblatt \(1952\)](#), [Dawid \(1984\)](#) and [Diebold et al. \(1998\)](#), we evaluate the density relative to the “true” but unobserved density using the probability integral transform (pits). The pits summarize the properties of the densities, and may help us to judge whether the densities are biased in a particular direction, and whether the width of the densities have been roughly correct on average. More precisely, the pits represent the ex-ante inverse predictive cumulative distribution evaluated at the ex-post actual observations.

A density is correctly specified if the pits are uniform, identically and, for one-step ahead forecasts, independently distributed. Accordingly, we may test for uniformity and independence at the end of the evaluation period. Several candidate tests exist, but few offer a composite test of uniformity and independence together, as would be appropriate for one-step ahead forecasts. In general, tests for uniformity are not independent of possible dependence and vice versa. Since the appropriateness of the tests are uncertain, we conduct several different tests. See [Hall and Mitchell \(2007\)](#) for elaboration and description of different tests.

We use a test of uniformity of the pits proposed by [Berkowitz \(2001\)](#). The Berkowitz test works with the inverse normal cumulative density function transformation of the pits. Then we can test for normality instead of uniformity. For 1-step ahead forecasts, the null hypothesis is that the transformed pits are identically and independently normally distributed, iid  $N(0,1)$ . The test statistics is  $\chi^2$  with three degrees of freedom. For longer horizons, we do not test for independence. In these cases, the null hypothesis is that the transformed pits are identically, normally distributed,  $N(0,1)$ . The test statistics is  $\chi^2$  with two degrees of freedom. Other tests of uniformity are the Anderson-Darling (AD) test (see [Noceti et al. \(2003\)](#)) and a Pearson chi-squared test suggested by [Wallis \(2003\)](#). Note that the two latter tests are more suitable for small-samples. Independence of the pits is tested by a Ljung-Box test, based on autocorrelation coefficients up to four for one-step ahead forecasts. For forecast horizons  $h > 1$ , we test for autocorrelation at lags equal to or greater than  $h$ .

## 4 Empirical exercise and ordering of data blocks

Our recursive forecasting exercise is intended to mimic the behavior of a policymaker now-casting in real-time. We use real-time data vintages for the U.S. economy for all forecasts and realizations (see section 2 for details). A key issue in this exercise is the choice of benchmark representing the “actual” measure of GDP. [Stark and Croushore \(2002\)](#) suggest three alternative benchmark data vintages: the most recent data vintage, the last vintage before a structural revision (called benchmark vintages) and finally the vintage that is released a fixed period of time after the first release. We follow [Clark and McCracken \(2010\)](#) and [Jore et al. \(2010\)](#) and use the second available estimate of GDP as actual.<sup>13</sup>

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<sup>13</sup>Our results are highly robust to using the fifth and the last vintage of GDP as actuals, see section 5.3.3 for more details.

We perform a real-time out-of-sample density nowcasting exercise for quarterly U.S. GDP growth. The recursive forecast exercise is constructed as follows: We estimate each model on a real-time sample and compute model nowcast/backcast for GDP. For each vintage of GDP we re-estimate all models and compute predictive densities (for all individual models, model classes and the combination) for every new data release within the quarter of interest (nowcast) until the first estimate of GDP is released. This will be approximately 3 weeks after the end of the quarter. By then the nowcast has turned into a backcast for that quarter.

The data we consider are either of monthly or quarterly frequency. Data series that have similar release dates and are similar in content are grouped together in blocks. Hence, some blocks of data will be updated every month, while others are only updated once every quarter. In total we have defined 15 different blocks, where the number of variables in each block varies from 30 in “Labor Market” to only 2 in “Money & Credit”.<sup>14</sup>

In Table 2, we illustrate the data release calendar and depict how the 15 different blocks are released throughout any month and quarter until the first release of GDP is available. The table shows for each model class the number of individual models that update their nowcast after every new data release. It also illustrates if the GDP nowcast is a two-step ahead or a one-step ahead forecast. Note that since all the individual models in the VAR class are of quarterly frequency, their nowcasts only change three times per quarter. That is whenever a full quarter of CPI inflation, interest rates or GDP is available. Nowcasts from the leading indicator model (LIM) class and the factor model (FM) class are, on the other hand, updated for every single new data release. However, while nowcasts from all the 12 factor models are updated for every new data release, only nowcasts from a fraction of the leading indicator models are updated. That is, only models that include the newly released data will update their nowcasts. This illustrates a key difference between how the density nowcasts from the FM class and the LIM class are revised. Where the nowcast from the FM class changes for every data release (since the factors are affected), the nowcast from the LIM class only changes if the newly released data contains information that historically has improved the log score. That is, if the models that revise their nowcast have a non-zero weight.

Finally, note that release lags vary for the different data series, ranging from 2 months for

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<sup>14</sup>On some dates more than one block is released, however our results are robust to alternative ordering of the blocks.

Table 2. *Structure of data releases and models updated from the start of the quarter until the first estimate of GDP is released.*

	Release	Block	Time	Horizon	Number of models updated				
					VAR	Indicator	Factor	Combination	
Nowcast	1	Interest rate	January	2	72	9	12	93	
	2	Financials		2		36	12	48	
	3	Surveys 2		2		18	12	30	
	4	Labor market		2		90	12	102	
	5	Money & Credit		2		6	12	18	
	6	Mixed 1		2		15	12	27	
	7	Ind. Production		2		48	12	60	
	8	Mixed 2		2		33	12	45	
	9	PPI		2		21	12	33	
	10	CPI		2		144	39	12	123
	11	GDP		1			360	12	516
	12	GDP & Income		1			21	12	33
	13	Housing		1			9	12	21
	14	Survey 1		1			12	12	24
	15	Initial Claims		1			3	12	15
	16	Interest rate	February	1		9	12	21	
	17	Financials		1		36	12	48	
	18	Surveys 2		1		18	12	30	
	19	Labor market		1		90	12	102	
	20	Money & Credit		1		6	12	18	
	21	Mixed 1		1		15	12	27	
	22	Ind. Production		1		48	12	60	
	23	Mixed 2		1		33	12	45	
	24	PPI		1		21	12	33	
	25	CPI		1		39	12	51	
	26	GDP		1					
	27	GDP & Income		1		21	12	33	
	28	Housing		1		9	12	21	
	29	Survey 1		1		12	12	24	
	30	Initial Claims		1		3	12	15	
31	Interest rate	March	1			9	12	21	
32	Financials		1			36	12	48	
33	Surveys 2		1			18	12	30	
34	Labor market		1			90	12	102	
35	Money & Credit		1			6	12	18	
36	Mixed 1		1			15	12	27	
37	Ind. Production		1			48	12	60	
38	Mixed 2		1			33	12	45	
39	PPI		1			21	12	33	
40	CPI		1			39	12	51	
41	GDP		1						
42	GDP & Income		1			21	12	33	
43	Housing		1			9	12	21	
44	Survey 1		1			12	12	24	
45	Initial Claims		1			3	12	15	
Backcast	46	Interest rate	April	1	72	9	12	93	
	47	Financials		1		36	12	48	
	48	Surveys 2		1		18	12	30	
	49	Labor market		1		90	12	102	
	50	Money & Credit		1		6	12	18	
	51	Mixed 1		1		15	12	27	
	52	Ind. Production		1	48	12	60		
	53	Mixed 2		1	33	12	45		
	54	PPI		1	21	12	33		
	55	CPI		1	144	39	12	123	
	56	GDP		1		360	12	516	

*Note: The table illustrates a generic quarter of our real-time out of sample forecasting experiment. Our forecast evaluation period runs from 1990Q2 to 2010Q3, which gives us more than 80 observations to evaluate for each data release. All models that are updated are re-estimated at each point in time throughout the quarter. In total we re-estimate and simulate the individual models well over 3000 times during a given quarter.*

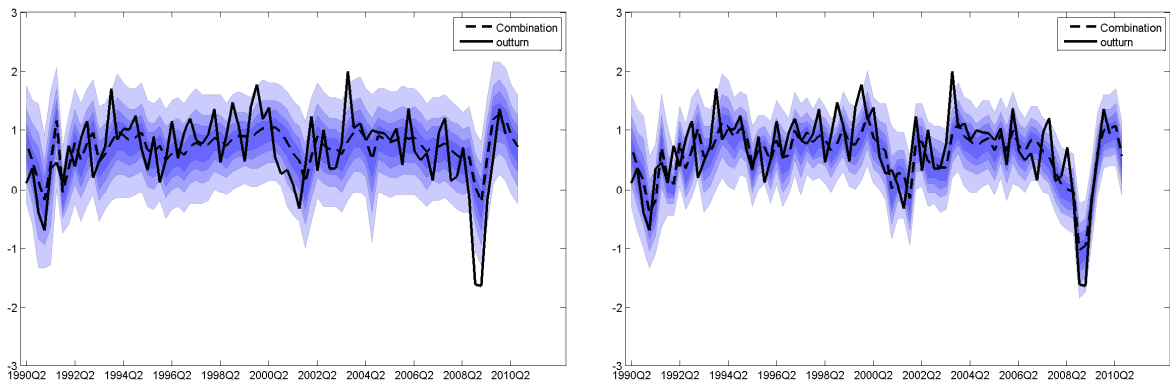
imports and exports data to current month for Business outlook surveys. Thus, the structure of the unbalancedness changes when a new block is released.

## 5 Results

In this section, we analyze the performance of our two-stage density nowcast combination approach. The main goal of our exercise is to study how the predictive densities improve as more data are available throughout the quarter. In doing so, we want to evaluate both the accuracy of the density nowcasts, section 5.1, and if they are well-calibrated, section 5.2.

In essence, our results and exercise can be illustrated by figure 1. The figure shows recursive real-time out-of-sample density nowcasts for U.S. GDP for the period 1990Q2-2010Q3. The nowcasts are made at two different points in time during the quarter. Recursive nowcasts made at the first day of the quarter are shown in the left panel, while recursive nowcasts made at the last day of the quarter are shown in the right panel. From the two panels in the figure we can clearly see how the predictive densities are better centered around the outturn as more information becomes available. This may indicate that more information improves the density nowcasts in terms of a higher log score.

Figure 1. Recursive real-time out-of-sample density nowcasts for quarterly U.S. GDP

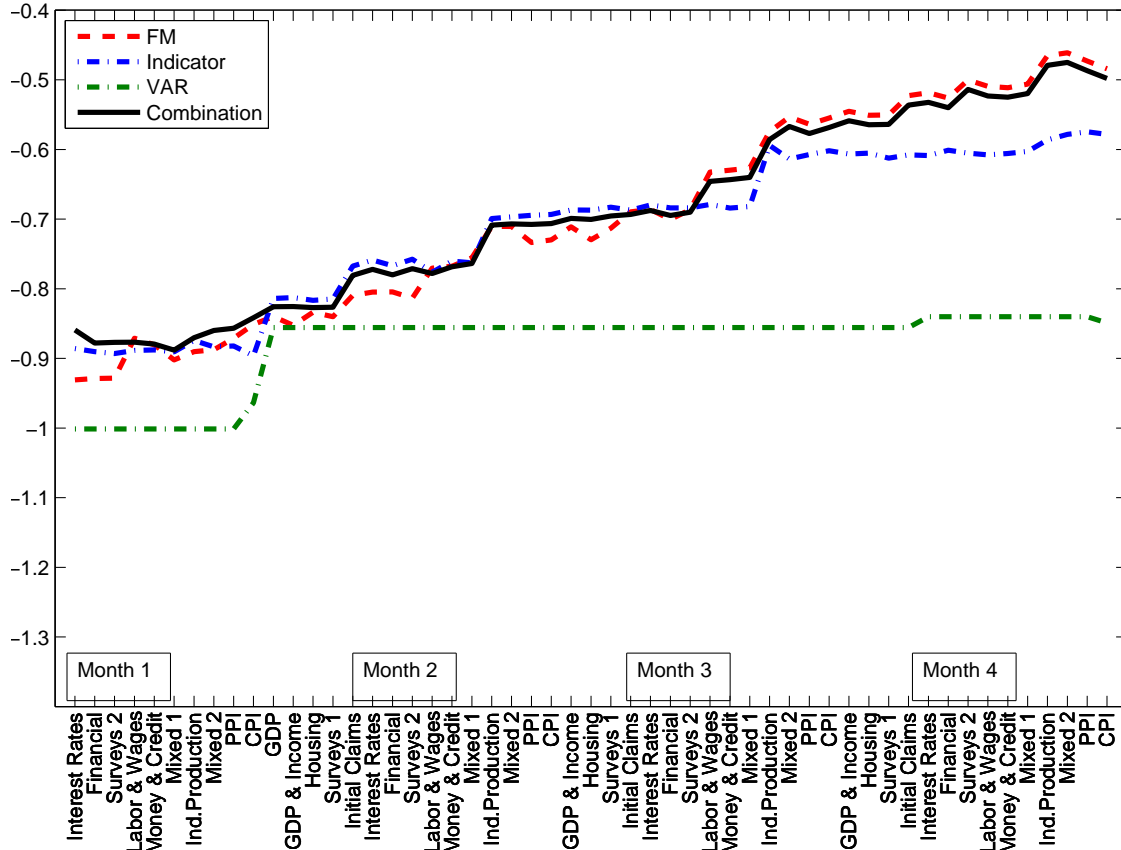


(a) Beginning of quarter ( $M0$ )

(b) End of quarter ( $M3$ )

*Note: The figures show recursive real-time out-of-sample density nowcasts for the quarterly U.S. GDP, made at two different points in time.  $M0$  refers to nowcasts made at the first day of the representing quarter, while  $M3$  refers to nowcasts made at the last day of the representing quarter. The solid line shows the second release of GDP. The shaded areas represent, respectively 30, 50, 70 and 90 per cent probability bands.*

Figure 2. Average log scores for forecasts after different block releases. Evaluated against 2nd release of data



Note: The individual models within each model class and the model classes have been combined using the linear opinion pool and log score weights. The evaluation period runs from 1990Q2 to 2010Q3.

### 5.1 Log score performance

We study the impact of different data releases on the density nowcasting/backcasting precision, measured by the average log score. Figure 2 depicts the average log scores for the nowcasts from the combined model and the three model classes after every data block release over the evaluation period. The 10 first observations of the quarter are actually two step ahead forecasts, while the 11 last observations are essentially backcasts, see table 2.

The figure reveals two interesting results. First, the forecasting performance improves when new information becomes available. The log score of the predictive densities for the model combination and all three model classes increases as new information arrives during the quarter. Second, the ranking of the model classes changes during the quarter and in



accordance with new data releases, while the model combination is always performing well. In fact, the average log score from the model combination is almost identical to the best performing model class throughout the quarter. The latter illustrates the main advantage of using forecast combinations. These results are remarkable robust to choice of “actual” GDP. While the performance of the different model classes and what data releases that improve the nowcast the most varies depending on the choice of benchmark (real-time vintage), the forecast combination is always performing very well. See section 5.3 for more on this.

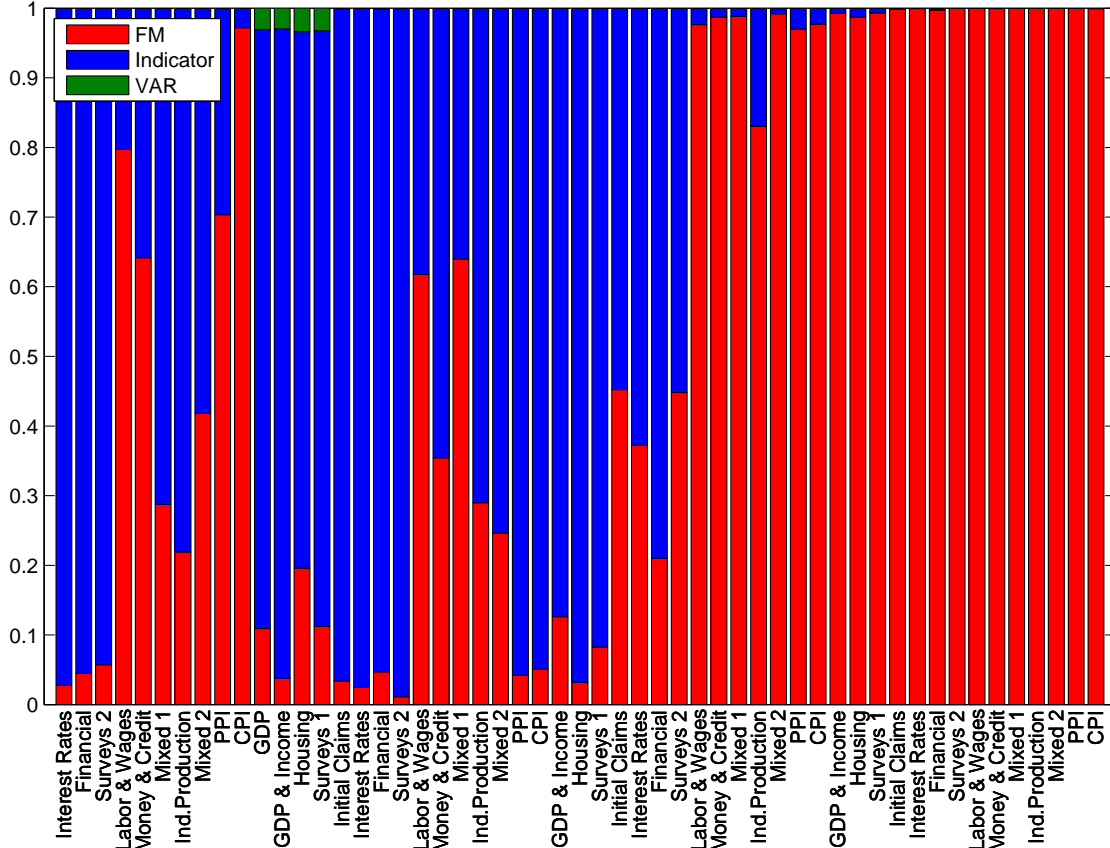
It is also worth noting that the LIM class and FM class are outperforming the VARs. This is clearly a result of their informational advantage, as the VARs only utilize quarterly data. Only immediately after GDP is released, the VARs perform on a par with the FM class. As new information arrives throughout the quarter, the leading indicator and factor models adapt faster than the VARs. This highlights the importance of utilizing higher frequency and non-synchronous data releases for nowcasting. Finally, figure 8 in the appendix shows in more detail how the different data releases improve the combined nowcasts as well as the nowcasts from the three model classes. The blocks of data that improves the nowcasts the most are “Ind. Production” and “Initial Claims”.

In figure 3, we depict the weights attached to each model class in the combined density forecast after every data block release. The figure illustrates the time-varying weights at the end of the evaluation period. As we would expect from figure 2 there are large changes in the weights throughout the quarter. The LIM class has a high weight in the early periods of the quarter, while the FM class gets higher weight as we move further into the quarter.<sup>15</sup> Towards the end of the quarter, the factor models ends up having almost all the weight. The reader should however not interpret this as attaching all weight to one unique model, as the FM class is a combination of 12 factor models. The VAR models seem to get very little weight throughout the quarter. Again, this must be seen as a result of their informational disadvantage relative to the factor models and leading indicator models.

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<sup>15</sup>Note, that labor market data tends to increase the weight attached to the FM class, while GDP releases seem to increase the weight attached to the LIM class.

Figure 3. *End of sample weights attached to the different model classes after different block releases. Evaluated against 2nd release of data*



*Note: The individual models within each model class and the model classes have been combined using the linear opinion pool and log score weights. The evaluation period runs from 1990Q2 to 2010Q3.*

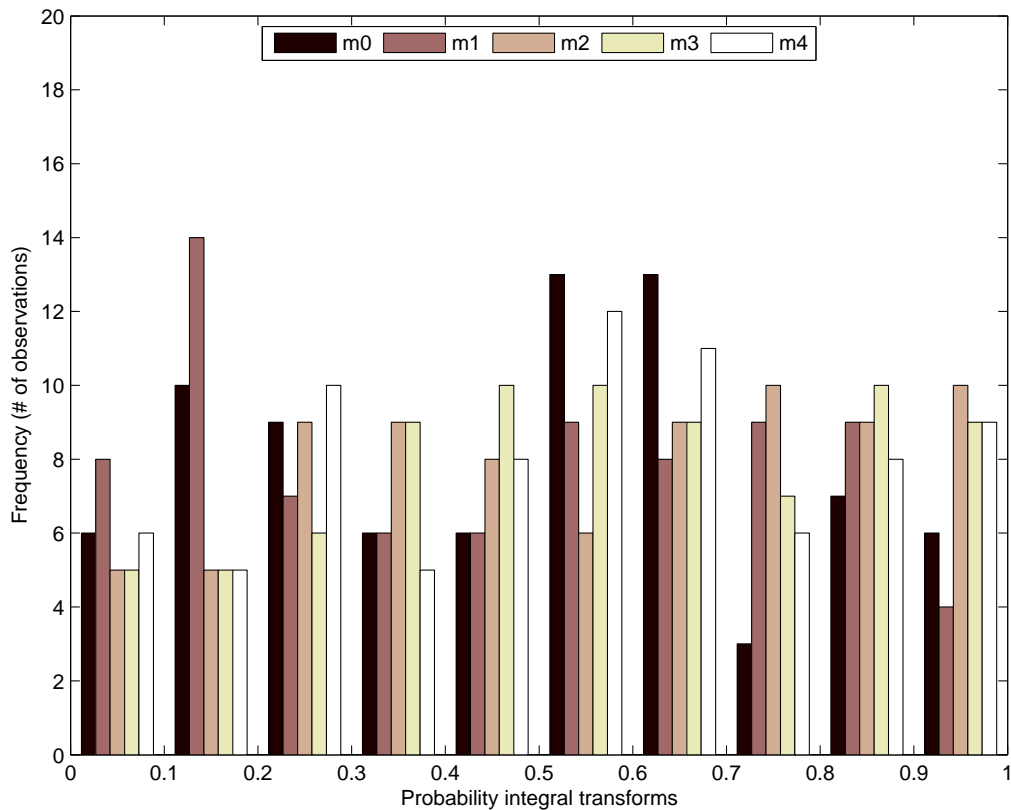
## 5.2 Testing the pits

We evaluate the predictive densities relative to the “true” but unobserved density using the pits of the realization of the variable with respect to the nowcast densities, see figure 4. Table 3 shows p-values for the four different tests, described in section 3.2, applied to the combined forecast at five different points in time ( $M0 - M4$ ).<sup>16</sup> P-values equal to or higher than 0.05 mean that we can not reject the hypothesis that the combination is correctly calibrated at a 95% significance level.

The predictive densities of the combined forecast passes all tests for horizon  $M0$ . This is the case where the nowcast corresponds to a two-step ahead forecast. Turning to the one-step

<sup>16</sup>To save space, we only report test results for the final combined density. More results are available upon request.

Figure 4. *Pits of the combined density forecast at five points in the quarter. The pits are the ex ante inverse predictive cumulative distributions evaluated at the ex post actual observations.*



Note: The pits of predictive densities should have a standard uniform distribution if the model is correctly specified. The  $M0$  bars refers to the 1th release of a generic quarter (see table 2), while  $M1$ ,  $M2$ ,  $M3$  and  $M4$  refer respectively to release 15, 30, 45 and 57.

ahead forecast ( $M1 - M4$ ), the predictive densities of the combined forecast also seem to be well-calibrated. Based on the Berkowitz test, the Anderson-Darling test and the Pearson chi-squared test, we cannot reject the null hypothesis that the combination is well-calibrated at a 95% significance level.<sup>17</sup>

<sup>17</sup>The null hypothesis in the Ljung-Box test is rejected at horizon  $M4$ .

Table 3. Pits tests for evaluating density forecasts for GDP (p-values)

	LogScore	Berkowitz	Wallis	Ljung-Box	Anderson-Darling
m0 nowcast	-0.89	<b>0.82</b>	<b>0.27</b>	<b>0.61</b>	<b>0.67</b>
m1 nowcast	-0.77	<b>0.65</b>	<b>0.73</b>	<b>0.53</b>	<b>0.46</b>
m2 nowcast	-0.69	<b>0.40</b>	<b>0.87</b>	<b>0.30</b>	<b>0.26</b>
m3 nowcast	-0.54	<b>0.21</b>	<b>0.76</b>	<b>0.20</b>	<b>0.25</b>
m4 backcast	-0.54	<b>0.46</b>	<b>0.30</b>	0.00	<b>0.43</b>

*Note: The null hypothesis in the Berkowitz test is that the inverse normal cumulative distribution function transformed pits are identically, normally distributed,  $N(0,1)$ , and for  $h = 1$  independent.  $\chi^2$  is the Pearson chi-squared test suggested by Wallis (2003) of uniformity of the pits histogram in eight equiprobable classes. Ljung-Box is a test for independence of the pits (in the first power) at lags greater than or equal to the horizon. The Anderson-Darling test is a test for uniformity of the pits, with the small-sample (simulated) p-values computed assuming independence of the pits.*

### 5.3 Robustness

As already noted, our results are robust to changes in the ordering of data releases.<sup>18</sup> In this section we perform three additional robustness checks: First, with respect to alternative weighting schemes. Second, with respect to point forecasting. Finally, we check for robustness with respect to choice of benchmark vintage for GDP.

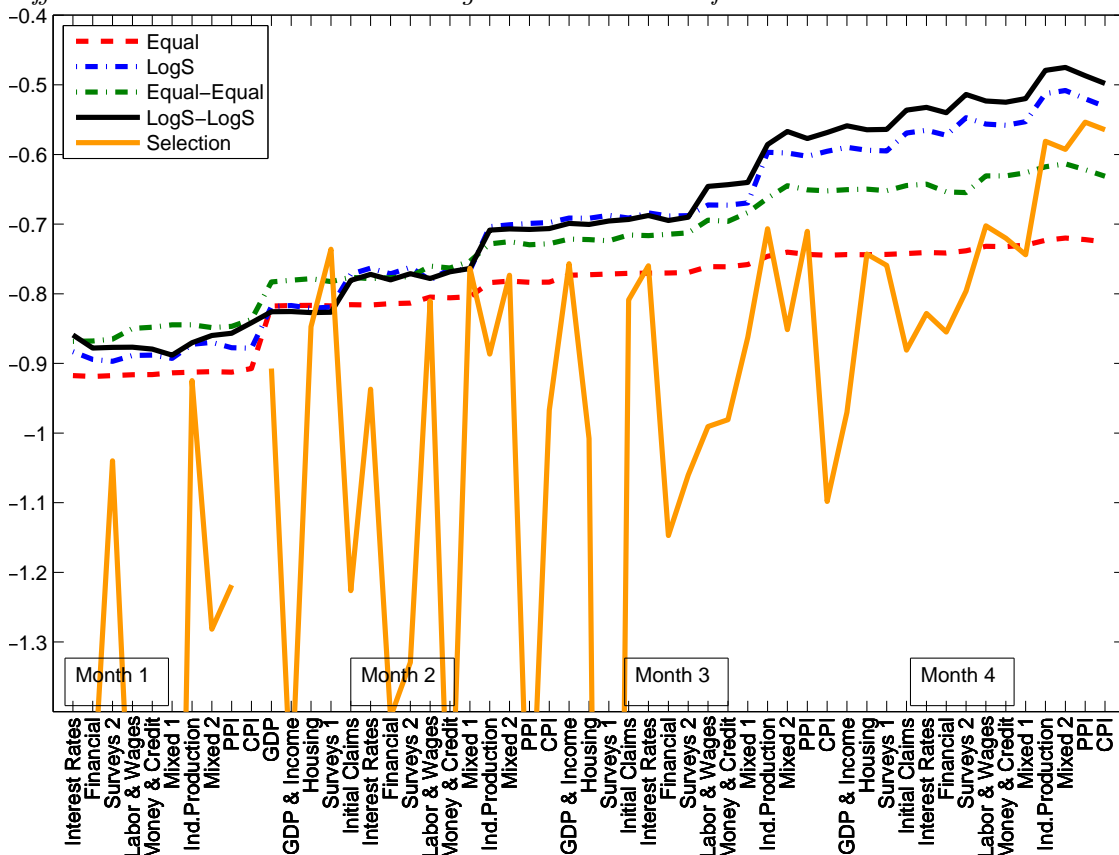
#### 5.3.1 Alternative weighting schemes for the combination

Several papers have found that simple combination forecasts, as equal weights, outperform more sophisticated adaptive forecast combination methods. This is often referred to as the forecast combination puzzle. While Jore et al. (2010) and Gerdrup et al. (2009) seem to find some evidence of gains from adaptive log score weights for density combination, this is still a question of debate. We check for robustness with respect to the following different weighting schemes: 1) combination of all models applying equal weights (Equal) and 2) combination of all models applying log score weights (LogS) and c) two-stage nowcast combination with equal weights in both stages (Equal-Equal) and 4) a selection strategy where we try to pick the “best” model. We have constructed this by recursively “picking” the best model among all the 516 models at each point in time throughout the evaluation period, and used this

<sup>18</sup>The results can be given on request.

to forecast the next period.<sup>19</sup> The preferred two-stage nowcast combination with log score weights in both stages is denoted as LogS-LogS.

Figure 5. *Comparing different weighting schemes. Average log scores for forecasts after different block releases. Evaluated against 2nd release of data*



Note: Equal and LogS denote that all individual models are combined using linear opinion pool and respectively equal weights or log score weights. Equal-Equal and LogS-LogS denotes that the individual models within each model class and the combination have been combined using the linear opinion pool and respectively equal weights and log score weights. Selection refers to a strategy of “picking” the best model among all the 516 models at each point in time throughout the evaluation period. The evaluation period runs from 1990Q2 to 2010Q3.

<sup>19</sup>In practice this is often the strategy that is employed when model combination is not conducted. As new models are tested and developed, they outstrip and replace the older models as time goes by. Our baseline real-time model combination experiment tries to be as honest as possible in this respect, by not replacing any of the 516 individual models during the evaluation period. However, the selection strategy we test is of course rather extreme, as we for each new data release and quarter do a selection based on the historical performance up to that point in time.

Figure 5 compares the average log score for the different weighting schemes. There are five interesting results. First, all combination methods yield a steady increase in the average log score as more information becomes available. This is not the case for the selection strategy, which gives large and volatile changes in the average log score after every data block release. Second, the selection strategy seems to almost always give the poorest density nowcast in terms of having the lowest average log score. Third, the difference between “Equal” and “Equal-Equal” can be seen as the “pure” gain from using a two-stage approach where models are first grouped into model classes and then combined together. It is evident from the figure that “Equal-Equal” is always performing better than “Equal”. Fourth, there is less differences between the “LogS” and “LogS-LogS”, as the log score weights discriminate rather sharply between nowcasts from the different models. Finally, no weighting scheme is superior throughout the quarter, but our preferred two-stage combination approach (“LogS-LogS”) is the best performing strategy for most of the quarter.

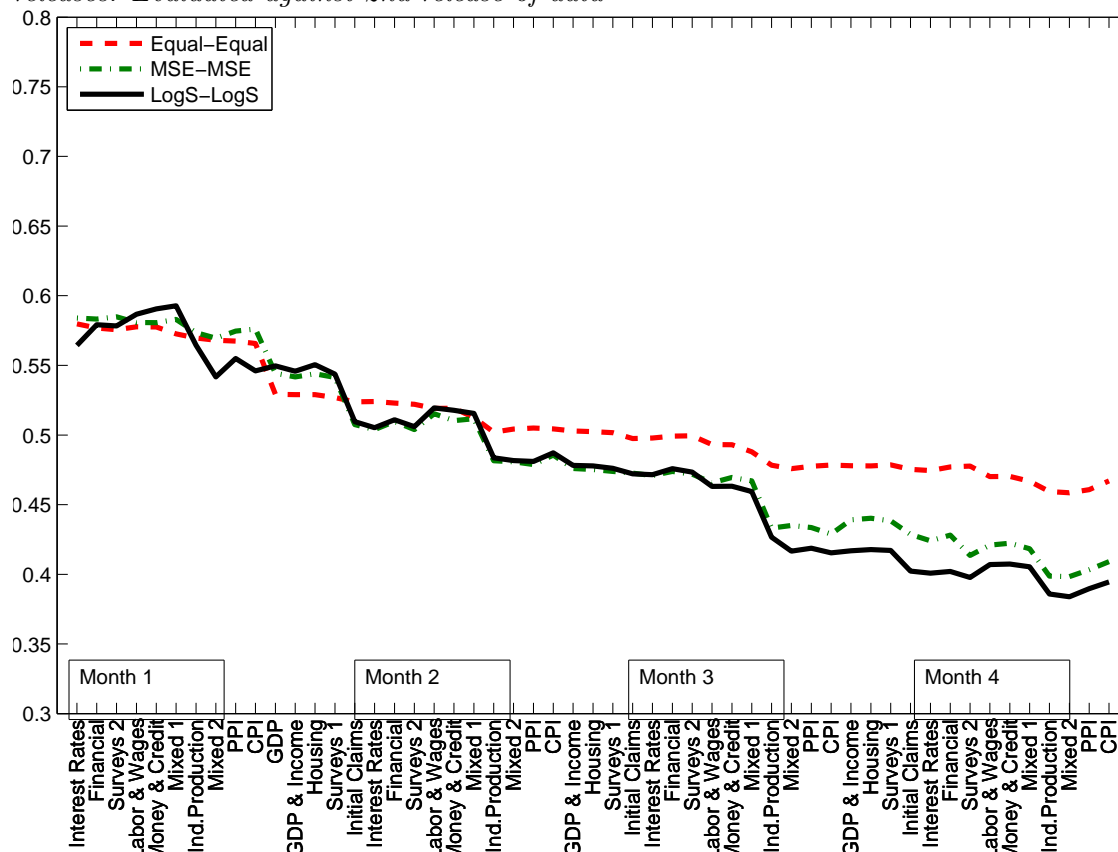
### 5.3.2 Point forecasting

Although the main purpose of this paper is to evaluate density nowcasts, we do check for robustness of our results with respect to point nowcasting performance. We do this by comparing three different combination strategies. In the first strategy we follow the two stage density combination strategy explained above, but calculate the final point nowcasts as the center of the final combined density nowcast. In the second strategy we calculate the point nowcasts for each single model as the center of the predictive density already before we combine the models in the first stage. We then use inverse mean squared errors (MSE) to calculate weights between the models within each model class, as well as between the three different model classes, see section 3.1.2. Finally, we calculate final point nowcast using a strategy where we apply equal weights to all models in both stages. For all three strategies we evaluate the final point forecasts using the root mean squared prediction error (RMSE). The rest of the experiment is similar to what is explained earlier.

Figure 6 depicts the RMSE for the combined nowcasts from the three strategies after every data block release. The figure displays two interesting results.

First, for all strategies the nowcasting errors are steadily reduced as more information becomes available throughout the quarter and until the first estimate of GDP is released.

Figure 6. Comparing different weighting schemes. RMSE for forecasts after different block releases. Evaluated against 2nd release of data



Note: Equal-Equal, MSE-MSE and LogS-LogS denotes that the individual models within each model class and the models classes have been combined using the linear opinion pool and respectively equal weights, MSE weights and log score weights. The evaluation period runs from 1990Q2 to 2010Q3.

This result is in accordance with what have been found in earlier nowcasting experiments using mean squared prediction error evaluation.<sup>20</sup>

Second, the density combination framework actually performs better in terms of point forecast evaluation than standard point forecast combination methods. It is very interesting to see that the pure density combination approach (“LogS-LogS”) actually scores better than

<sup>20</sup>In the appendix we also show how the different model classes perform using the point forecast strategy, see figure 7. The ranking of the model classes is changing throughout the quarter while the combined nowcasts is always performing very well, which resembles the results we report for the pure density combination approach. Our results also support the finding in Giannone et al. (2008), i.e. that factor models are performing well in terms of point nowcast. However, note that FM in the figure denotes the nowcast from the FM class and not from one specific factor model. That is, a nowcast combination of 12 different factor models.

the MSE strategy also in terms of MSE. As far as we are aware of, this is a new finding in the nowcasting literature. We think the result is linked to the properties of the log score weights. As new information arrives throughout the quarter, the log score weights adapt faster than standard point forecast weights (e.g. MSE weights). In this way, our combination procedure attaches a higher weight to models with new and relevant information. This finding motivates the potential leverage of density evaluation over simple point forecast evaluation when the goal is to maximize forecast accuracy in a nowcasting framework.

### 5.3.3 Alternative benchmark vintages

The choice of benchmark vintage is a key issue in any application using real-time vintage data.<sup>21</sup> In our application, we use the 2nd available vintage of GDP as benchmark. Figure 10 and Figure 11 in the appendix shows results with respectively the 5th release of GDP and the last available vintage of GDP as benchmark. Clearly the figures show that the nowcasting performance of the different model classes varies with choice of benchmark vintage. Hence, also the weights attached to the different model classes varies. However, the result that the density combination nowcast is always performing well, seems to be remarkably robust. This implies that there are additional gains from combining forecasts in a real-time environment where the forecast target (benchmark) is not obvious.

## 6 Conclusion

In this paper we have used a density combination framework to produce density combination nowcasts for U.S. quarterly GDP growth from a system of three different model classes widely used at central banks; VARs, leading indicator models and factor models. The density nowcasts are combined in a two-step procedure. In the first step, we group models into different model classes. The nowcasts for each model within a model class are combined using the log score. This yields a combined predictive density nowcast for each of the three different model classes. In a second step, these three predictive densities are combined into a new density nowcast using the log score. The density nowcasts are updated for every new data release during a quarter until the first release of GDP is available. Our recursive nowcasting exercise

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<sup>21</sup>See [Croushore \(2006\)](#) for a survey on forecasting with real-time macroeconomic data.



is applied to U.S. real-time data and evaluated on the period 1990Q2-2010Q3.

We show that the log scores for the predictive densities increase almost monotonically as new information arrives during the quarter. The densities also seem to be well-calibrated. Further, while the ranking of the model classes is changing during the quarter and in accordance with new data releases, the model combination is always performing well. Finally, the density combination approach is superior compared to a simple model selection strategy, and the density combination framework actually performs better in terms of point forecast evaluation than standard point forecast combination methods. All our results illustrate the potential gains from using a density combination approach in a nowcasting environment.

Interestingly these results are very robust to the use of benchmark (real-time) vintage. While the nowcasting performance from different model classes may vary according to the benchmark vintage, the density combination nowcast is always performing very well. This implies that there are additional gains from combining forecasts in a real-time environment where the forecast target or the benchmark is not obvious.

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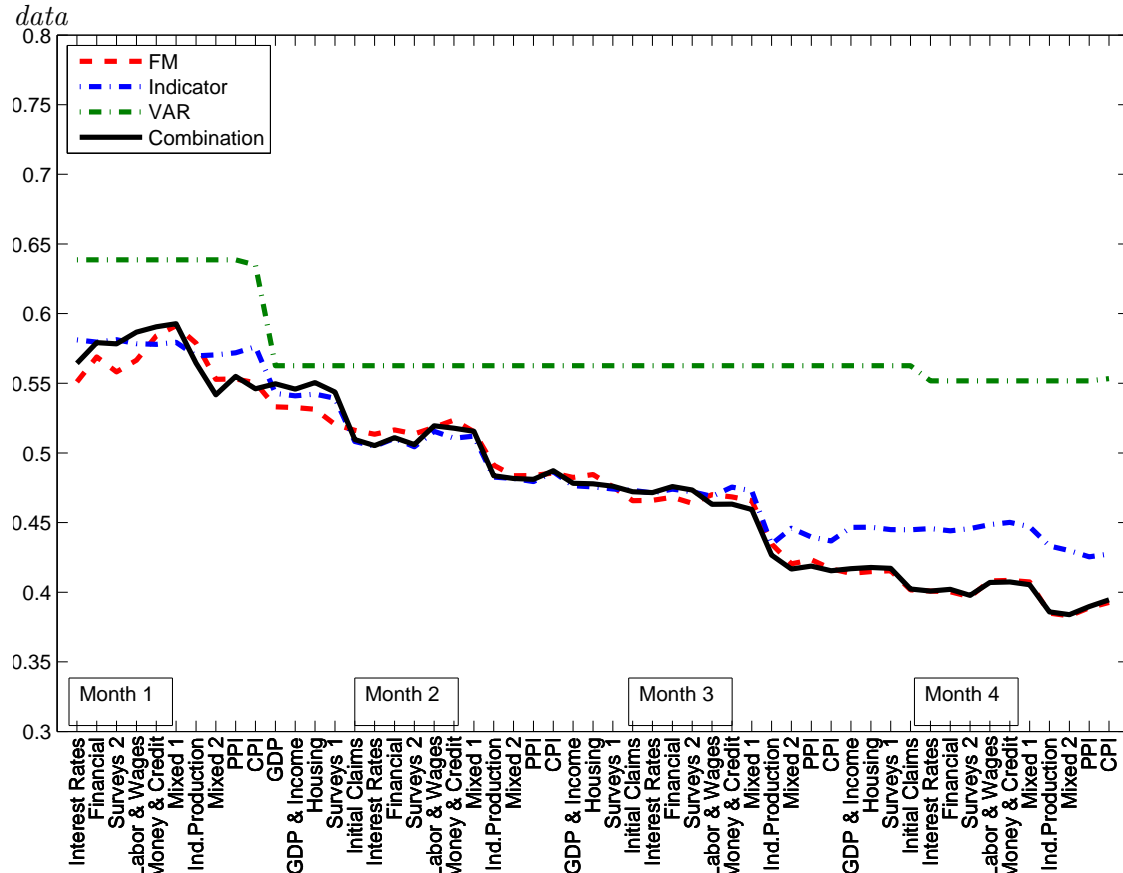
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## 7 Appendix

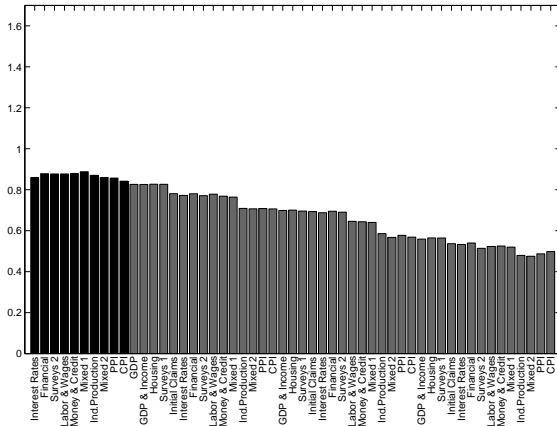
### 7.1 Robustness

Figure 7. *RMSE for forecasts after different block releases. Evaluated against 2nd release of data*

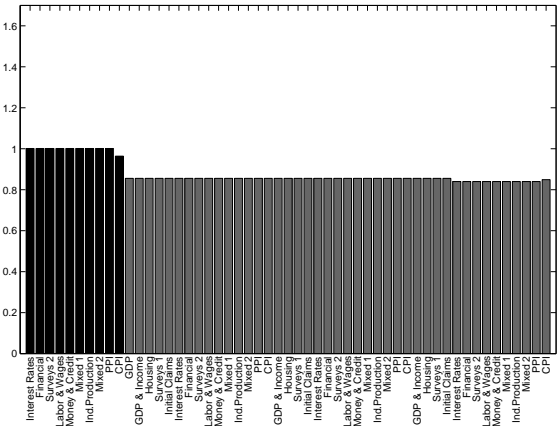


*Note: The individual models within each model class and the model classes have been combined using the linear opinion pool and log score weights. The evaluation period runs from 1990Q2 to 2010Q3.*

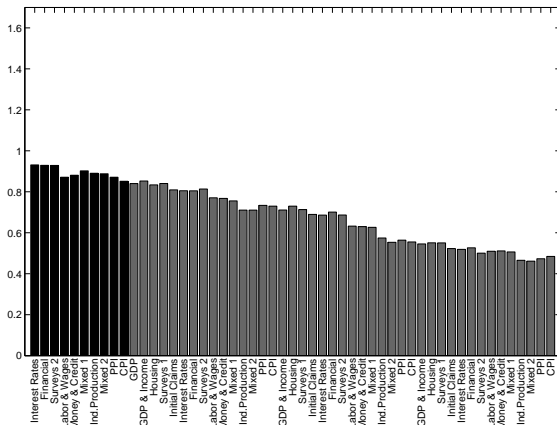
Figure 8. Average log scores (inverted) for forecasts after different block releases. Evaluated against 2nd release of data.



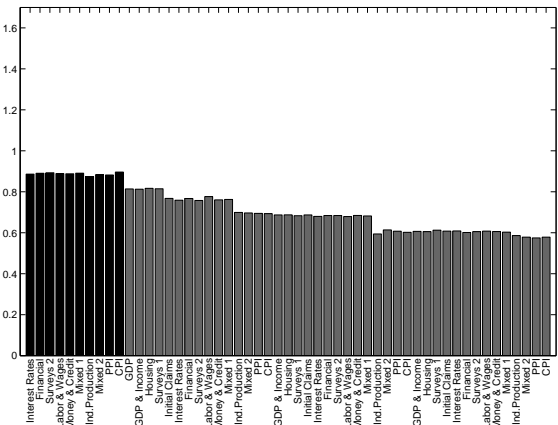
(a) Combined forecast



(b) VARs



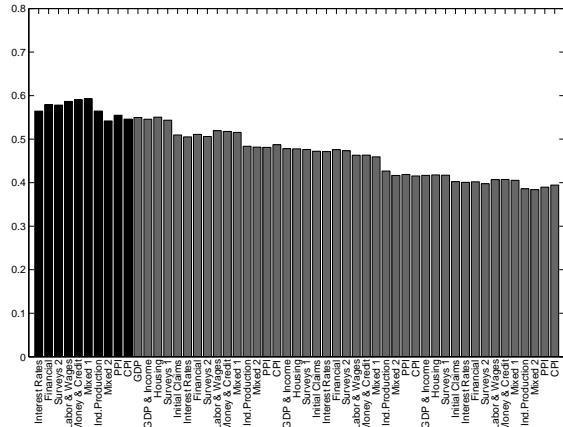
(c) FM



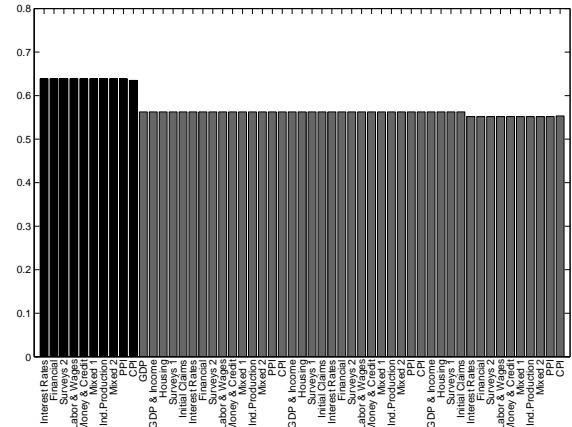
(d) Indicator

*Note: The individual models within each model class and the model classes have been combined using the linear opinion pool and log score weights. The evaluation period runs from 1990Q2 to 2010Q3.*

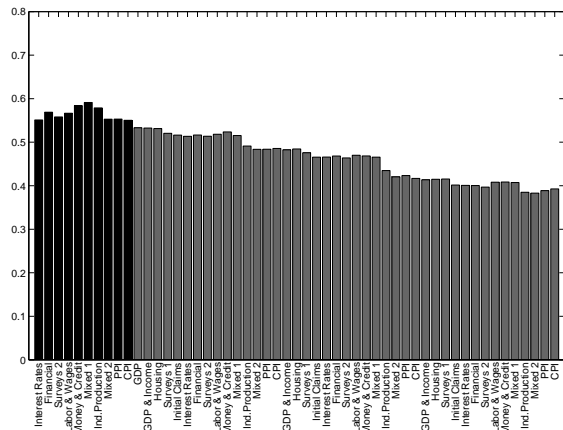
Figure 9. Mean square forecasting errors made after different block releases. Evaluated against 2nd release of data.



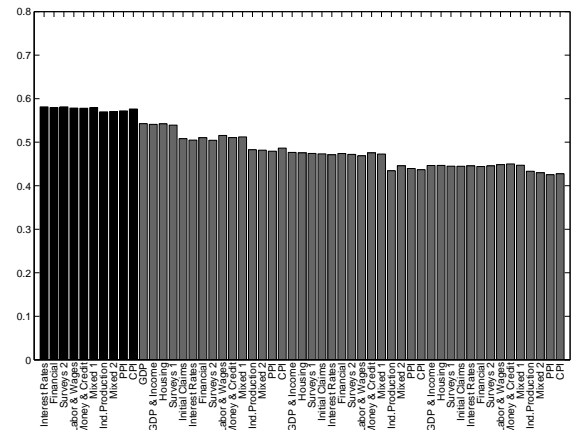
(a) Combined forecast



(b) VARs



(c) FM

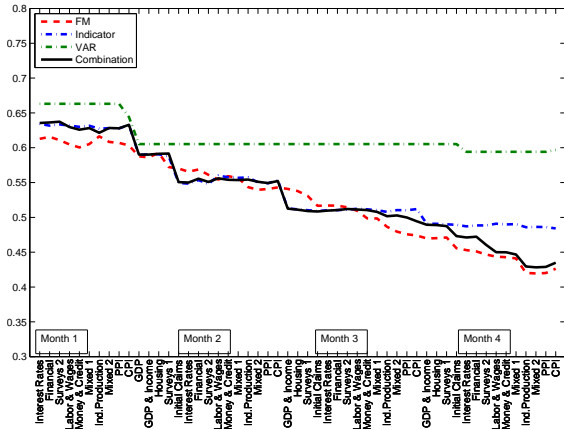


(d) Indicator

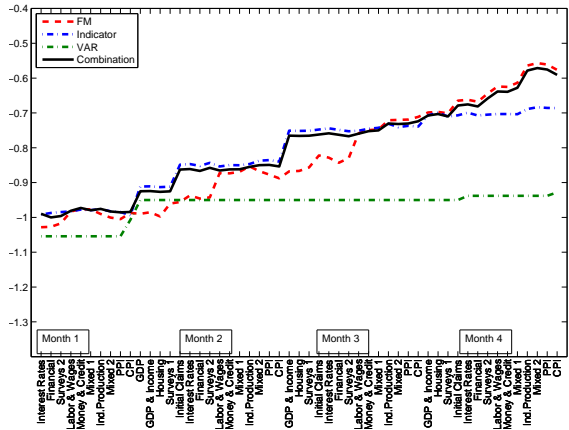
*Note: The individual models within each model class and the model classes have been combined using the linear opinion pool and log score weights. The evaluation period runs from 1990Q2 to 2010Q3.*



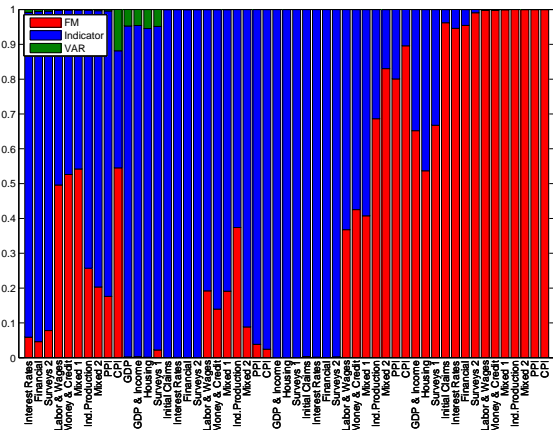
Figure 10. Results when evaluated against 5th release of data.



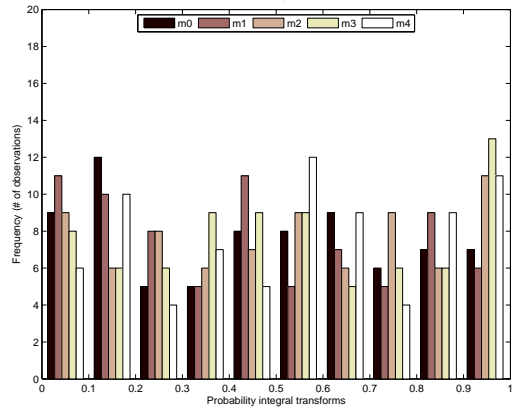
(a) RMSE



(b) Average log score



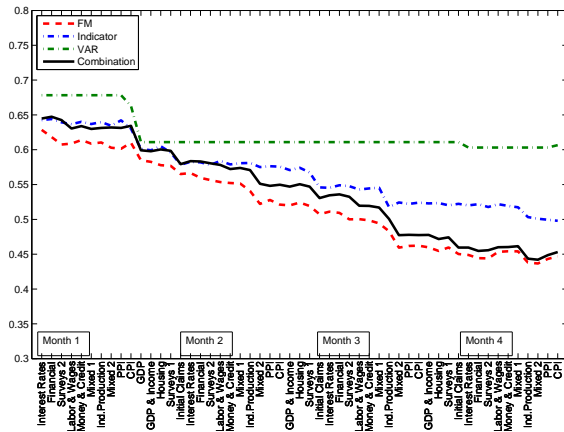
(c) Weights



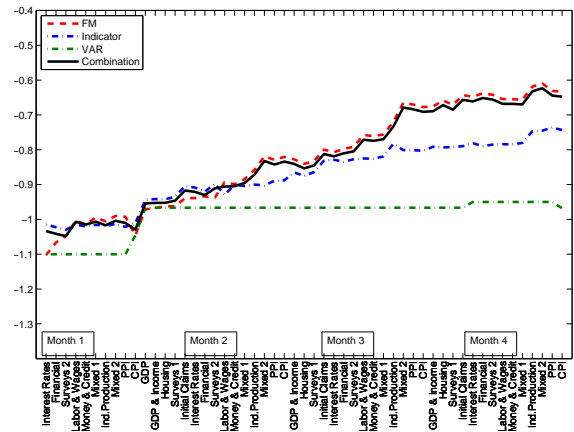
(d) Pits

Note: The individual models within each model class and the model classes have been combined using the linear opinion pool and log score weights. The evaluation period runs from 1990Q2 to 2010Q3.

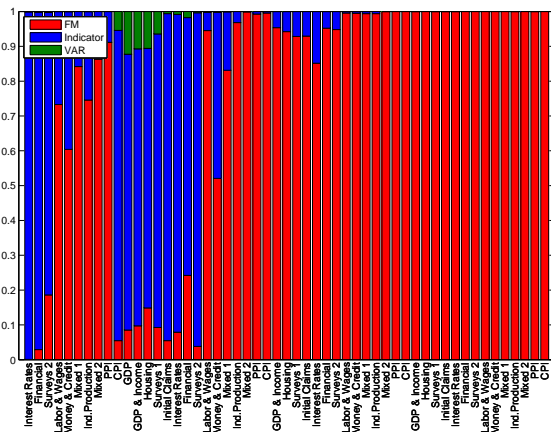
Figure 11. Results when evaluated against last available vintage of data.



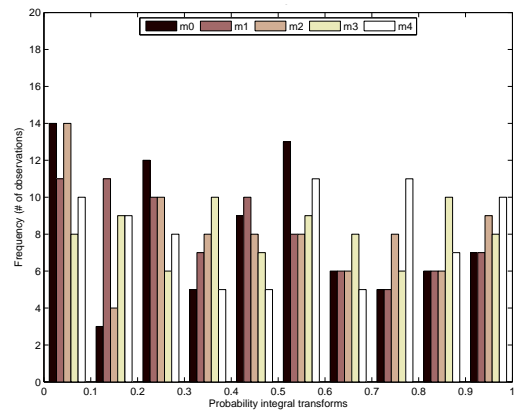
(a) RMSE



(b) Average log score



(c) Weights



(d) Pits

Note: The individual models within each model class and the model classes have been combined using the linear opinion pool and log score weights. The evaluation period runs from 1990Q2 to 2010Q3.

## 7.2 Models and model classes

Table 1 in the main text gives a brief description of the three model classes and individual models within each class that are included in this analysis. A more thorough description of each model class and the different specifications is given below.

### 7.2.1 Vector Autoregressive models (VAR)

VAR models, first introduced by Sims (1980), are arguably the most commonly used model class for economic analysis and forecasting by policymakers. Assume we have the following general model

$$Y_t = \alpha + \sum_{i=1}^p \beta_i Y_{t-i} + \epsilon_t, \quad \epsilon_t \sim N(0, \Sigma_\epsilon), \quad (8)$$

where  $Y_t = (y_{1,t}, y_{2,t})$ . We include four different quarterly VAR models, where  $y_{1,t}$  always denotes GDP, while  $y_{2,t}$  is either empty (AR model) or contains CPI inflation and/or the Federal funds rate. For each of the four models we consider three different transformations of the data; first differences, double differences and detrended (using an exponential smoother). As VARs may be prone to instabilities, both full-sample and two different rolling-sample VARs are estimated. The two rolling-samples are set to 20 and 30 quarters. Finally, we let the lag length  $p$  vary from 1 to 4. In total, we consider 36 AR models, 72 bivariate VARs and 36 trivariate VARs. We refer to these models as the *VARs*.

Several papers such as, Evans (2005), Giannone et al. (2008) and Aruoba et al. (2009), show that accounting for the timeliness of data is crucial for nowcasting. That is, the exploitation of timely information leads to improvement in the nowcast accuracy. Taking into account the flow of data releases is therefore essential to our analysis. In the case of the VARs, both quarterly CPI inflation and quarterly averages of the Federal funds rate are available prior to the GDP release. The models are put into a state space form and hence Kalman filter techniques can easily be applied to deal with missing data, i.e. the unbalanced data problem. This is also a key aspect when constructing the predictive densities from the different models. The forecast uncertainties are obtained through simulations, where the final densities are derived using kernel smoothing techniques. By applying the Kalman filter we can obtain conditional forecasts when the data set is unbalanced. More precisely, we use the smoothed covariance matrix of the predictors, which will resemble the mean squared error

(MSE) matrix of the system, and draw from the normal distribution to obtain simulated forecasts for each horizon.<sup>22</sup> This is explained in more detail in appendix section 7.3.

### 7.2.2 Leading indicator models (LIM)

There is a large amount of studies showing that leading indicators are useful for economic forecasting, see among others [Banerjee et al. \(2005\)](#), [Banerjee and Marcellino \(2006\)](#) and [Marcellino \(2006\)](#) for a survey on the use of leading indicators in macroeconomics.

We include in total 120 leading indicators for U.S. GDP. For each leading indicator we construct a bivariate VAR as described in equation 8, where  $y_{2,t}$  now will denote the leading indicator. As with the VARs, both full-sample and two different rolling-sample models are estimated. The rolling-samples are set to 20 and 30 quarters. All the leading indicators included here are of monthly frequency. Hence, we need to bridge the monthly indicators with quarterly GDP. This is done by constructing quarterly averages of the monthly series. If a monthly series only contains one or two months of a quarter, we simply construct the average of the one or two observations from the quarter of interest.<sup>23</sup> The unbalanced data set problem and the construction of the predictive densities are then handled in the same way as described for the VARs above.

### 7.2.3 Factor Models (FM)

Factor models have become increasingly popular at central banks as they tend to have good forecasting properties, benefitting from exploiting information from large datasets. See among others [Stock and Watson \(2002\)](#) and [Giannone et al. \(2008\)](#).

The objective of factor models is to summarize the information contained in large datasets, while at the same time reducing their dimension. In other words; to reduce the parameter space. The model that we consider is an approximate dynamic factor model similar to [Giannone et al. \(2008\)](#). This is a model that accounts for the unbalanced data set problem. Assume we have a vector of  $n$  stationary monthly variables  $X_t = \left( x_{1t}, \dots, x_{nt} \right)'$ ,  $t = 1, \dots, T$ , which have been standardized to have mean equal to zero and variance equal to one. The

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<sup>22</sup>See for example [Lütkepohl \(2005\)](#).

<sup>23</sup>See [Baffigi et al. \(2004\)](#) and [Angelini et al. \(2011\)](#) for a more detailed discussion of alternative bridge equations.

model is given by the following two equations.

$$X_t = \chi_t + \xi_t = \Lambda F_t + \xi_t, \quad \xi_t \sim N(0, \Sigma_\xi) \quad (9)$$

$$F_t = \sum_{i=1}^p A_i F_{t-i} + B u_t, \quad u_t \sim N(0, I_u) \quad (10)$$

Equation 9 relates the monthly time series  $X_t$  to a common component  $\chi_t$  plus an idiosyncratic component  $\xi_t = (\xi_{1,t}, \dots, \xi_{n,t})'$ . The former is given by an  $r \times 1$  vector of latent factors  $F_t = (f_{1,t}, \dots, f_{r,t})'$  times an  $n \times r$  matrix of factor loadings  $\Lambda$ , while the latter is assumed to be multivariate white noise. Equation 10 describes the law of motion for the latent factors. The factors are driven by  $q$ -dimensional standardized white noise  $u_t$ , where  $B$  is an  $r \times q$  matrix, where  $q \leq r$ . Finally,  $A_1, \dots, A_p$  are  $r \times r$  matrices of parameters.

Our task is to nowcast quarterly GDP growth ( $y_t^Q$ ). We therefore need to build a bridge between the monthly variables and the quarterly GDP. All monthly variables are transformed to ensure that the corresponding quarterly quantities are given by  $x_{i,t}^Q \sim (x_{i,t} + x_{i,t-1} + x_{i,t-2})$  measured at the last month of each quarter, i.e.  $t = 3k$  and  $k = 1, \dots, T/3$ . This implies that series in differences enter the factor model in terms of three-month changes. Defining the quarterly factors as  $F_t^Q = (F_t + F_{t-1} + F_{t-2})$ , the factors-based bridge equation follows:

$$y_t^Q = \alpha + \beta' \widehat{F}_t^Q + e_t, \quad e_t \sim N(0, \Sigma_e) \quad (11)$$

where  $\beta$  is an  $r \times 1$  vector of parameters.

The model is estimated in a two-step procedure using principal components and the Kalman filter. The unbalanced part of the data set can be incorporated through the use of the Kalman filter, where missing observations are interpreted to have an infinitely large noise to signal ratio. For more details about this, see [Giannone et al. \(2008\)](#).

The simulated forecasts from the dynamic factor model are derived using a small modification of the technique described for the VARs above. The factors are derived and forecasted using the Kalman filter, while the forecasting equation itself is direct, and conditional on the factors. Uncertainty in the factor forecasts are taken into account in the forecasting equation. The factor uncertainty is drawn from the normal distribution, using the smoothed covariance matrix from the Kalman Filter in the same manner as described above. The uncertainty in the forecasting equation is derived through drawing a random shock from the normal distribution of past residuals.

### 7.3 The Kalman Filter: An example with a bivariate VAR

Assume we have the following bivariate VAR:

$$\begin{bmatrix} y_{1,t} \\ y_{2,t} \end{bmatrix} = \begin{bmatrix} c_1 \\ c_2 \end{bmatrix} + \begin{bmatrix} \beta_{11} & \beta_{12} \\ \beta_{21} & \beta_{22} \end{bmatrix} \begin{bmatrix} y_{1,t-1} \\ y_{2,t-1} \end{bmatrix} + \begin{bmatrix} u_{1,t} \\ u_{2,t} \end{bmatrix} \quad (12)$$

which can be written as:

$$Y_t = C + \beta Y_{t-1} + U_t \quad (13)$$

If we put our VAR into a State Space form we will get the following equations:

**State equation**

$$\alpha_t = \beta \alpha_{t-1} + C + U_t \quad (14)$$

**Observation equation**

$$Y_t = \alpha_t \quad (15)$$

In our application we have two different cases; a balanced VAR and an unbalanced VAR.

**Balanced VAR**

In the case with a balanced data set, we will have the following prediction equations

$$\alpha_{t|t-1} = \beta \alpha_{t-1|t-1} + C \quad (16)$$

$$P_{t|t-1} = \beta P_{t-1|t-1} \beta' + Q \quad (17)$$

$$v_{t|t-1} = Y_t - Y_{t|t-1} = Y_t - \alpha_{t|t-1} \quad (18)$$

$$F_{t|t-1} = P_{t-1|t-1} \quad (19)$$

and the following updating equations

$$\alpha_{t|t} = \alpha_{t|t-1} + K_t v_{t|t-1} \quad (20)$$

$$P_{t|t} = P_{t|t-1} - K_t Z_t P_{t|t-1} \quad (21)$$

In the case where we perfectly observe the state  $K = 1$ , while in the case where we are forecasting,  $K = 0$ . Note that the the variance of the prediction error increases when the forecasting horizon increases.

### Unbalanced VAR

Assume that we now observe  $y_{2,t}$ , but not  $y_{1,t}$ . In this case we have an unbalanced VAR. In this case the prediction equations 16 and 17 still holds, while equation 18 and 19 changes to

$$v_{t|t-1} = Y_t - Y_{t|t-1} = W_t Y_t - Z_t \alpha_{t|t-1} \quad (22)$$

with  $W_t = \begin{bmatrix} 0 \\ 1 \end{bmatrix}'$ , since  $Y_{1,t}$  is now not observed.

$$F_{t|t-1} = W_t P_{t-1|t-1} W_t' = \text{Var}(u_2) \quad (23)$$

and the following updating equations

$$\alpha_{t|t} = \alpha_{t|t-1} + K_t v_{t|t-1} = \alpha_{t|t-1} + P_{t|t-1} Z_t' W_t' F_{t|t-1}^{-1} v_{t|t-1} \quad (24)$$

$$P_{t|t} = P_{t|t-1} - K_t Z_t P_{t|t-1} = P_{t|t-1} - P_{t|t-1} Z_t' W_t' F_{t|t-1}^{-1} W_t Z_t P_{t|t-1} \quad (25)$$

Note that  $K_t = P_{t|t-1} Z_t' W_t' F_{t|t-1}^{-1} = \begin{bmatrix} \text{Cov}(u_1, u_2) \text{Var}(u_2)^{-1} \\ 1 \end{bmatrix}$

In other words  $K$  is equal to 1 in the equation which has one more observation ( $y_{2,t}$ ), since we observe the prediction error. While  $K$  will be a positive number between zero and one for the equation with the missing observation ( $y_{1,t}$ ). The stronger the covariance between the two error terms ( $u_{1,t}$  and  $u_{2,t}$ ), the higher will  $K$  be.

## 7.4 Data description

Block	Block Name	Description	Publication Lag	Start Vintage
1	Interest Rates	Federal funds rate	One month	Last vintage
1	Interest Rates	3 month Treasury Bills	One month	Last vintage
1	Interest Rates	6 month Treasury Bills	One month	Last vintage
2	Financials	Spot USD/EUR	One month	Last vintage
2	Financials	Spot USD/JPY	One month	Last vintage
2	Financials	Spot USD/GBP	One month	Last vintage
2	Financials	Spot USD/CAD	One month	Last vintage
2	Financials	Price of gold on the London market	One month	Last vintage
2	Financials	NYSE composite index	One month	Last vintage
2	Financials	Standard & Poors 500 composite index	One month	Last vintage
2	Financials	Standard & Poors dividend yield	One month	Last vintage
2	Financials	Standard & Poors P/E Ratio	One month	Last vintage
2	Financials	Moodys AAA corporate bond yield	One month	Last vintage
2	Financials	Moodys BBB corporate bond yield	One month	Last vintage
2	Financials	WTI Crude oil spot price	One month	Last vintage
3	Surveys 2	Purchasing Managers Index (PMI)	One month	03.03.1997
3	Surveys 2	ISM mfg index, Production	One month	02.11.2009
3	Surveys 2	ISM mfg index, Employment	One month	02.11.2009
3	Surveys 2	ISM mfg index, New orders	One month	02.11.2009
3	Surveys 2	ISM mfg index, Inventories	One month	02.11.2009
3	Surveys 2	ISM mfg index, Supplier deliveries	One month	02.11.2009
4	Labor Market	Civilian Unemployment Rate	One month	05.01.1990
4	Labor Market	Civilian Participation Rate	One month	07.02.1997
4	Labor Market	Average (Mean) Duration of Unemployment	One month	05.01.1990
4	Labor Market	Civilians Unemployed - Less Than 5 Weeks	One month	05.01.1990
4	Labor Market	Civilians Unemployed for 5-14 Weeks	One month	05.01.1990
4	Labor Market	Civilians Unemployed for 15-26 Weeks	One month	05.01.1990
4	Labor Market	Civilians Unemployed for 27 Weeks and Over	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Total nonfarm	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Total Private Industries	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Goods-Producing Industries	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Construction	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Durable goods	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Nondurable goods	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Manufacturing	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Mining and logging	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Service-Providing Industries	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Financial Activities	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Education & Health Services	One month	06.06.2003
4	Labor Market	Employment on nonag payrolls: Retail Trade	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Wholesale Trade	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Government	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Trade, Transportation & Utilities	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Leisure & Hospitality	One month	06.06.2003
4	Labor Market	Employment on nonag payrolls: Other Services	One month	05.01.1990
4	Labor Market	Employment on nonag payrolls: Professional & Business Services	One month	06.06.2003
4	Labor Market	Average weekly hours of PNW: Total private	One month	Last vintage
4	Labor Market	Average weekly overtime hours of PNW: Mfg	One month	Last vintage
4	Labor Market	Average weekly hours of PNW: Mfg	One month	Last vintage
4	Labor Market	Average hourly earnings:Construction	One month	Last vintage
4	Labor Market	Average hourly earnings: Mfg	One month	Last vintage
5	Money & Credit	M1 Money Stock	One month	30.01.1990
5	Money & Credit	M2 Money Stock	One month	30.01.1990
6	Mixed 1	Consumer credit: New car loans at auto finance companies, loan-to-value	Two months	Last vintage
6	Mixed 1	Consumer credit: New car loans at auto finance companies, amount financed	Two months	Last vintage
6	Mixed 1	Federal government total surplus or deficit	One month	Last vintage
6	Mixed 1	Exports of goods, total census basis	Two months	Last vintage



Block	Block Name	Description	Publication Lag	Start Vintage
6	Mixed 1	Imports of goods, total census basis	Two months	Last vintage
7	Ind. Production	Industrial Production Index	One month	17.01.1990
7	Ind. Production	Industrial Production: Final Products (Market Group)	One month	14.12.2007
7	Ind. Production	Industrial Production: Consumer Goods	One month	14.12.2007
7	Ind. Production	Industrial Production: Durable Consumer Goods	One month	14.12.2007
7	Ind. Production	Industrial Production: Nondurable Consumer Goods	One month	14.12.2007
7	Ind. Production	Industrial Production: Business Equipment	One month	14.12.2007
7	Ind. Production	Industrial Production: Materials	One month	14.12.2007
7	Ind. Production	Industrial Production: Durable Materials	One month	14.12.2007
7	Ind. Production	Industrial Production: nondurable Materials	One month	14.12.2007
7	Ind. Production	Industrial Production: Manufacturing (NAICS)	One month	14.12.2007
7	Ind. Production	Industrial Production: Durable Manufacturing (NAICS)	One month	14.12.2007
7	Ind. Production	Industrial Production: Nondurable Manufacturing (NAICS)	One month	14.12.2007
7	Ind. Production	Industrial Production: Mining	One month	14.12.2007
7	Ind. Production	Industrial Production: Electric and Gas Utilities	One month	14.12.2007
7	Ind. Production	Capacity Utilization: Manufacturing (NAICS)	One month	05.12.2002
7	Ind. Production	Capacity Utilization: Total Industry	One month	15.11.1996
8	Mixed 2	Housing starts: Total new privately owned housing units started	One month	18.01.1990
8	Mixed 2	New private housing units authorized by building permits	One month	17.08.1999
8	Mixed 2	Phily Fed Buisness outlook survey, New orders	Current month	Last vintage
8	Mixed 2	Phily Fed Buisness outlook survey, General business activity	Current month	Last vintage
8	Mixed 2	Phily Fed Buisness outlook survey, Shipments	Current month	Last vintage
8	Mixed 2	Phily Fed Buisness outlook survey, Inventories	Current month	Last vintage
8	Mixed 2	Phily Fed Buisness outlook survey, Unfilled orders	Current month	Last vintage
8	Mixed 2	Phily Fed Buisness outlook survey, Prices paid	Current month	Last vintage
8	Mixed 2	Phily Fed Buisness outlook survey, Prices received	Current month	Last vintage
8	Mixed 2	Phily Fed Buisness outlook survey, Number of employees	Current month	Last vintage
8	Mixed 2	Phily Fed Buisness outlook survey, Average workweek	Current month	Last vintage
9	PPI	Producer Price Index: Finished Goods	One month	12.01.1990
9	PPI	Producer Price Index: Finished Goods Less Food & Energy	One month	11.12.1996
9	PPI	Producer Price Index: Finished Consumer Goods	One month	11.12.1996
9	PPI	Producer Price Index: Intermediate Materials: Supplies & Components	One month	12.01.1990
9	PPI	Producer Price Index: Crude Materials for Further Processing	One month	12.01.1990
9	PPI	Producer Price Index: Finished Goods Excluding Foods	One month	11.12.1996
9	PPI	Producer Price Index: Finished Goods Less Energy	One month	11.12.1996
10	CPI	Consumer Prices Index: All Items (urban)	One month	18.01.1990
10	CPI	Consumer Prices Index: Food	One month	12.12.1996
10	CPI	Consumer Prices Index: Housing	One month	Last vintage
10	CPI	Consumer Prices Index: Apparel	One month	Last vintage
10	CPI	Consumer Prices Index: Transportation	One month	Last vintage
10	CPI	Consumer Prices Index: Medical care	One month	Last vintage
10	CPI	Consumer Prices Index: Commodities	One month	Last vintage
10	CPI	Consumer Prices Index: Durables	One month	Last vintage
10	CPI	Consumer Prices Index: Services	One month	Last vintage
10	CPI	Consumer Prices Index: All Items Less Food	One month	12.12.1996
10	CPI	Consumer Prices Index: All Items Less Food & Energy	One month	12.12.1996
10	CPI	Consumer Prices Index: All items less shelter	One month	Last vintage
10	CPI	Consumer Prices Index: All items less medical care	One month	Last vintage
11	GDP	Real Gross Domestic Product	One quarter	28.01.1990
12	GDP & Income	Real Disposable Personal Income	One month	29.01.1990
12	GDP & Income	Real Personal Consumption Expenditures	One month	29.01.1990
12	GDP & Income	Real Personal Consumption Expenditures: Durable Goods	One month	29.01.1990
12	GDP & Income	Real Personal Consumption Expenditures: Nondurable Goods	One month	29.01.1990
12	GDP & Income	Real Personal Consumption Expenditures: Services	One month	29.01.1990
12	GDP & Income	Personal Consumption Expenditures: Chain-type Price Index	One month	01.08.2000
12	GDP & Income	Personal Consumption Expenditures: Chain-Type Price Index Less Food & Energy	One month	01.08.2000
13	Housing	New one family houses sold	One month	30.07.1999
13	Housing	New home sales: Ratio of houses for sale to houses sold	One month	Last vintage
13	Housing	Existing home sales: Single-family and condos	One month	Last vintage

<b>Block</b>	<b>Block Name</b>	<b>Description</b>	<b>Publication Lag</b>	<b>Start Vintage</b>
14	Surveys 1	Chicago Fed MMI Survey	One month	Last vintage
14	Surveys 1	Composite index of 10 leading indicators	One month	Last vintage
14	Surveys 1	Consumer confidence surveys: Index of consumer confidence	Current month	Last vintage
14	Surveys 1	Michigan Survey: Index of consumer sentiment	Current month	31.07.1998
15	Initial Claims	Average weekly initial claims	Current month	Last vintage

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The objective of CAMP is to provide high quality research and analysis into the field of macroeconomics, as well as financial issues.

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